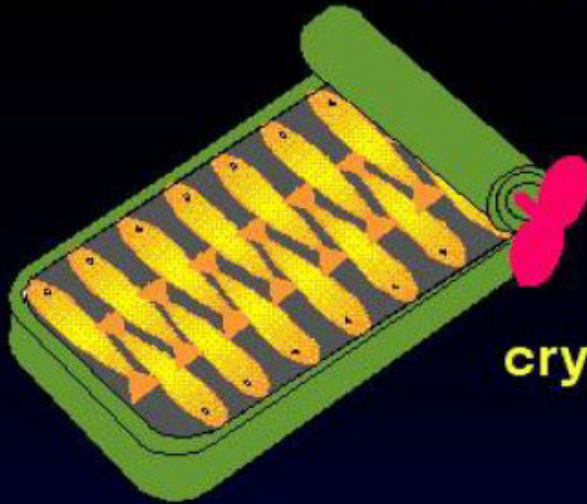


SAXS Refinement

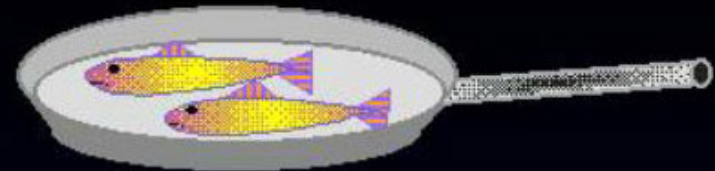
Willy Wriggers

School of Health Information Sciences &
Institute of Molecular Medicine
University of Texas – Houston

Structural Biology



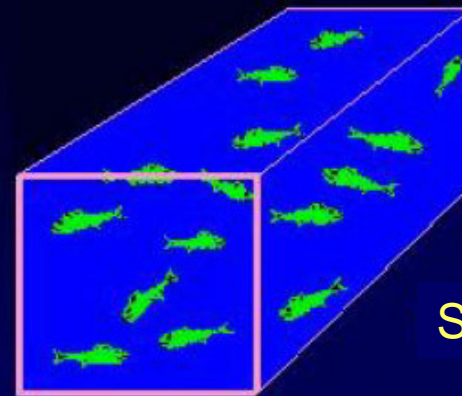
crystallography



electron microscopy



modelling

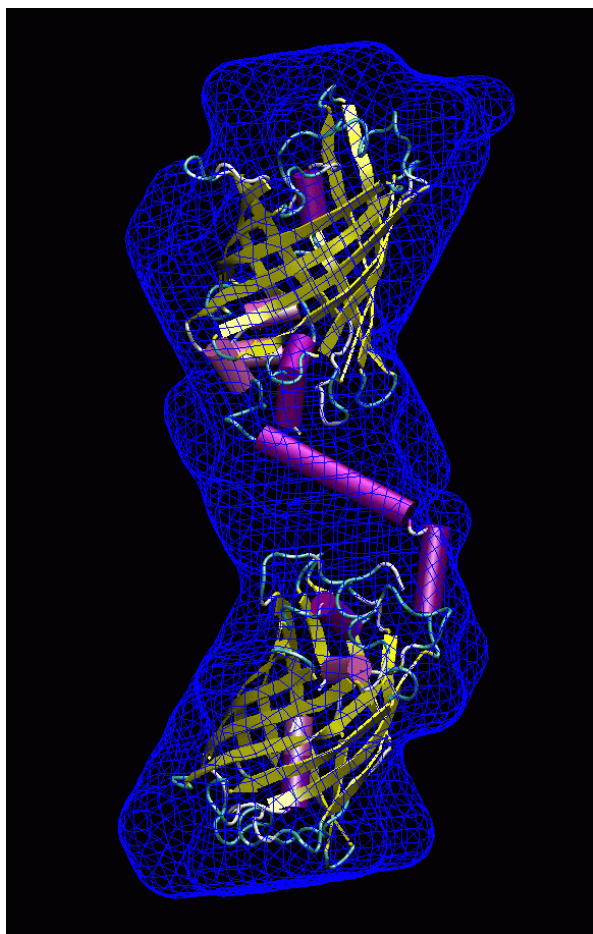


SAXS

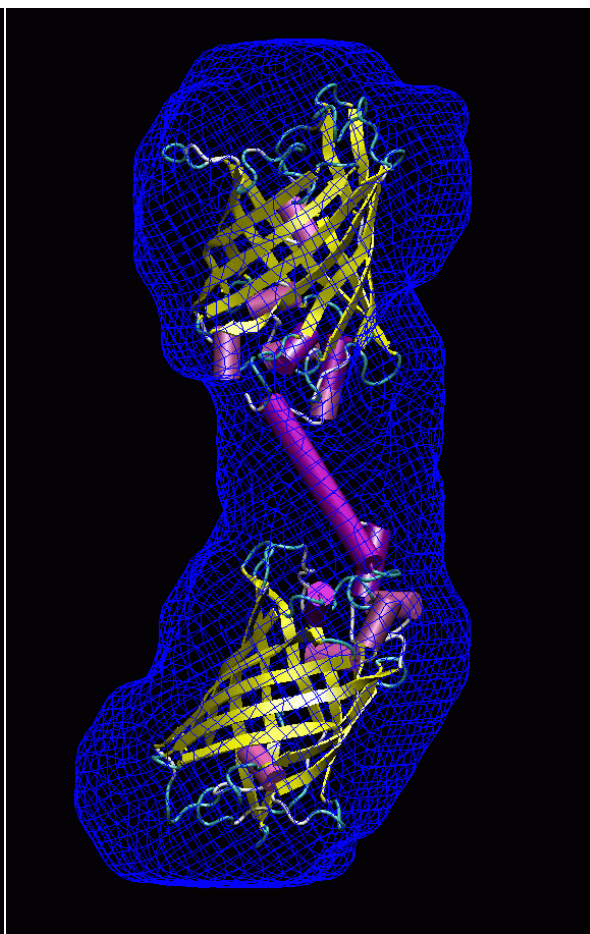


BL45 SAXS Station

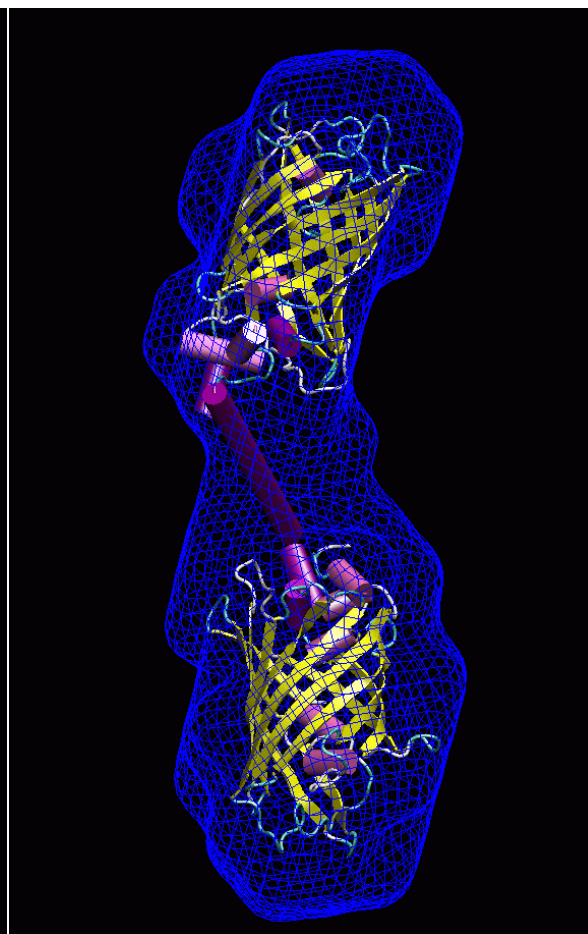
EBFP-linker-EGFP fusion proteins
(Tetsuro Fujisawa)



LAEEAAKEAAAKEAAAKAAA (20)



LAEEAAKEAAAKEAAAKEAAAKAAA (25)



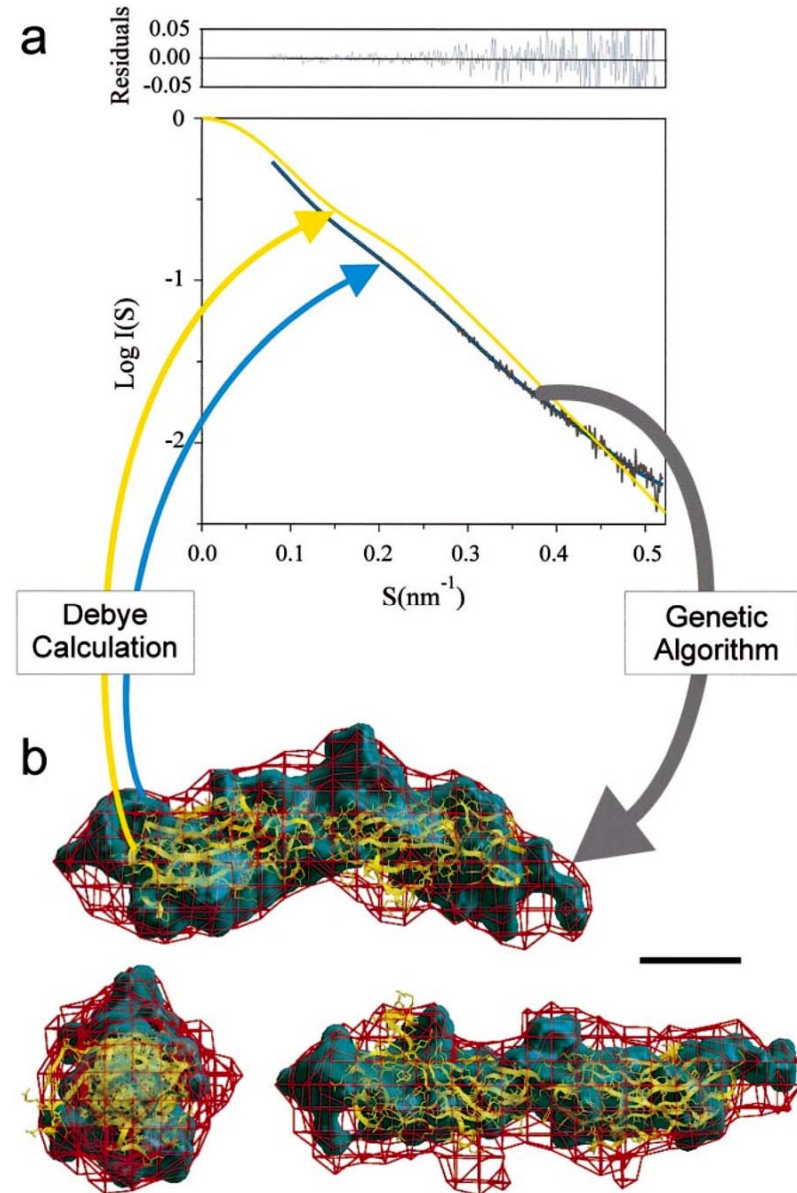
LAEEAAKEAAAKEAAAKEAAAKEAAAKAAA (30)

Generating 3D Structures from 1D SAXS Data

Low-resolution
3D shapes from
1D scattering profiles!

Small molecules OK!

Chacón et al., JMB (2000) 299:1289



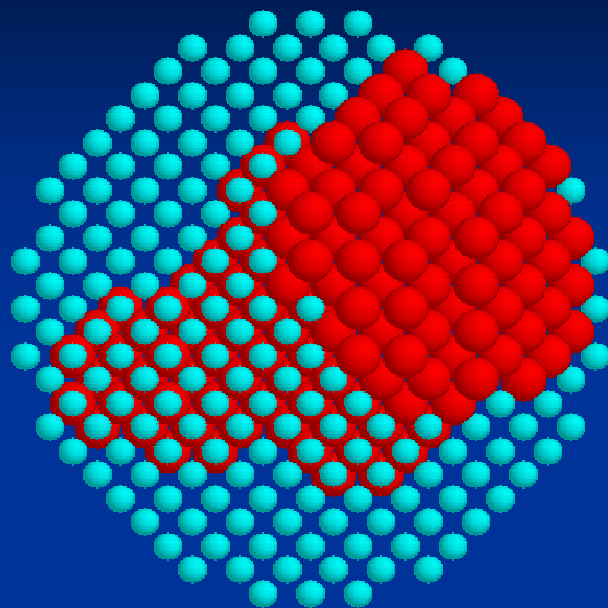
ab initio Methods



Envelope function

Stuhrmann, H. B. (1970) *Z. Physik. Chem. N.F.* **72**, 177

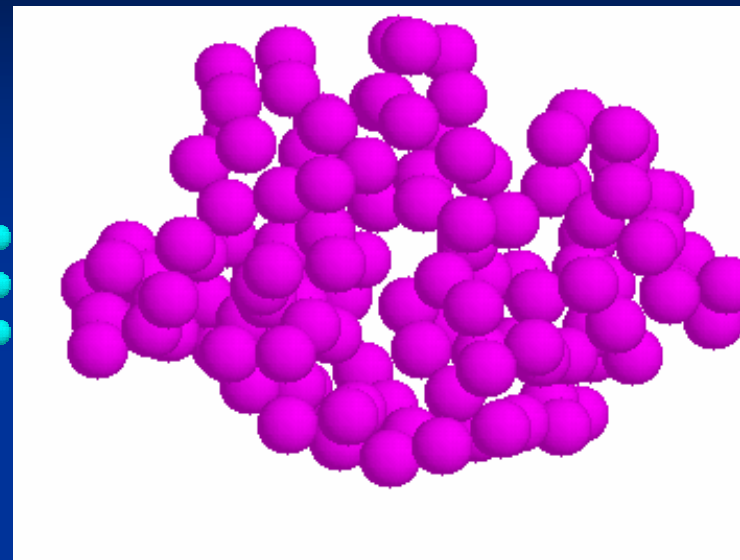
Svergun, D.I. *et al.* (1996) *Acta Crystallogr.* **A52**, 419



Bead models

Chacón, P. *et al.* (1998) *Biophys. J.* **74**, 2760

Svergun, D.I. (1999) *Biophys. J.* **76**, 2879



Dummy residues model

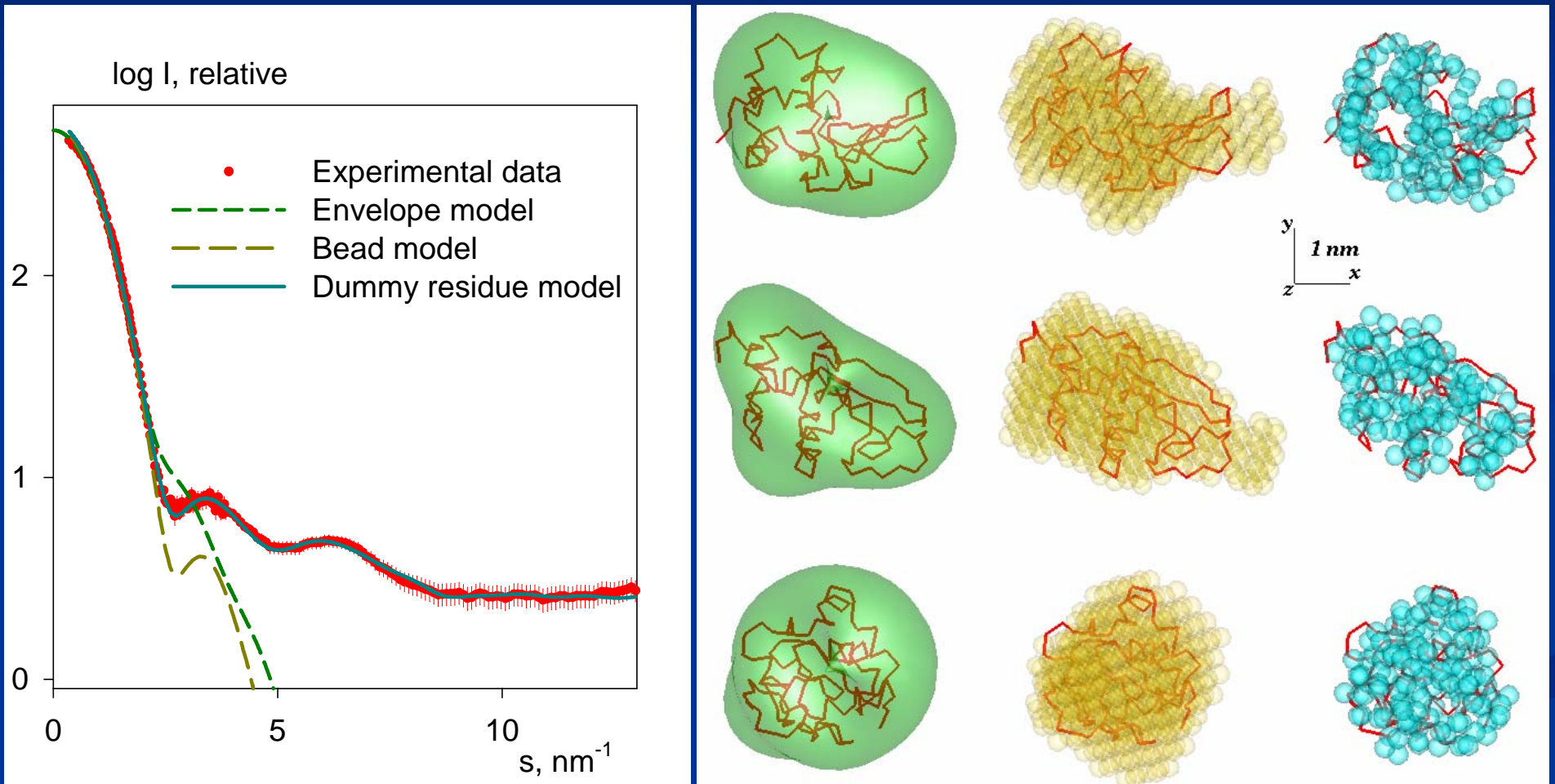
Svergun, D.I., Petoukhov, M.V. & Koch, M.H.J. (2001) *Biophys. J.* **80**, 2946-2953.

All the methods minimize $\text{Discrepancy}[\text{Data}] + \text{Penalty}[\text{Additional info}]$

© Dimitri Svergun

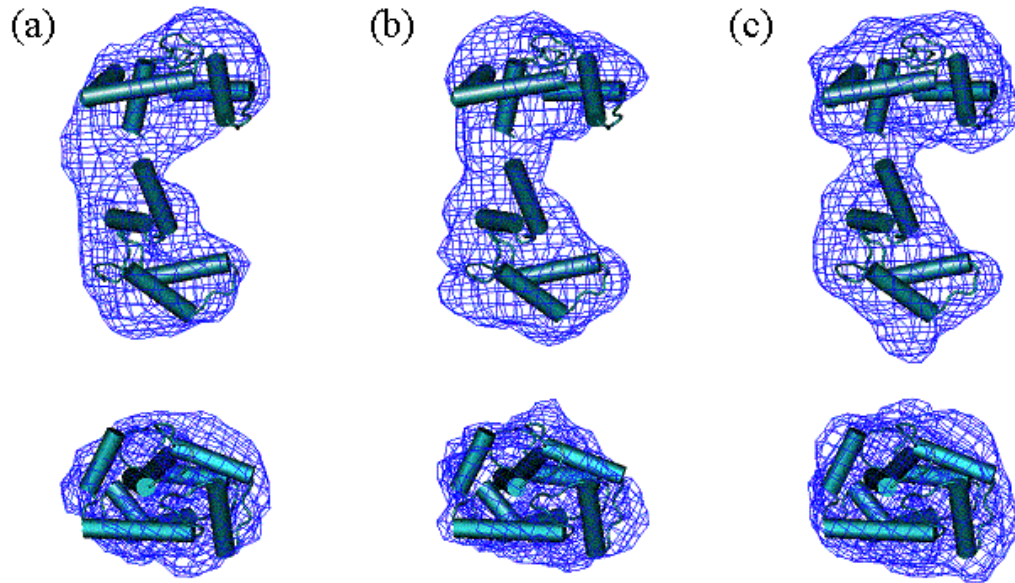
Benchmarking *ab initio* Methods

Envelope *Bead model* *Dummy residues*



Comparison with the crystal structure of lysozyme

How to Validate SAXS Bead Modeling?



Ab initio Shape Determination
using a Single Phase Dummy
Atom Model

by Simulated Annealing
(**DAMMIN**, Svergun)

by Genetic Algorithm
(**DALAI_GA**, Chacon)

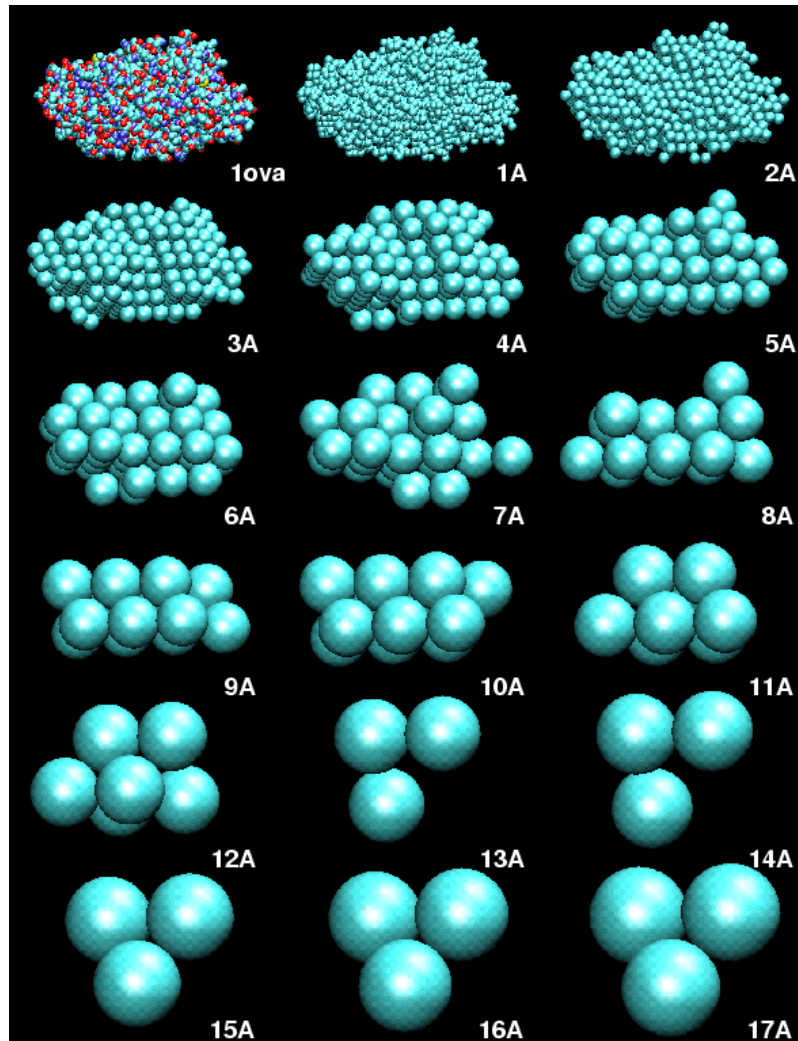
by Monte Carlo style give 'n' take
algorithm (**SAXS3D**, Walther)

Takahashi, Y., Nishikawa, Y., Fujisawa, T. Evaluation of three algorithms for ab initio determination of three-dimensional shape from one-dimensional solution scattering profiles, (2003) *J Appl Cryst*, **36**, 549-552.

Independent of algorithms, bead models converged to the average structure.

© Tetsuro Fujisawa

Simulated Bead Models for Validation

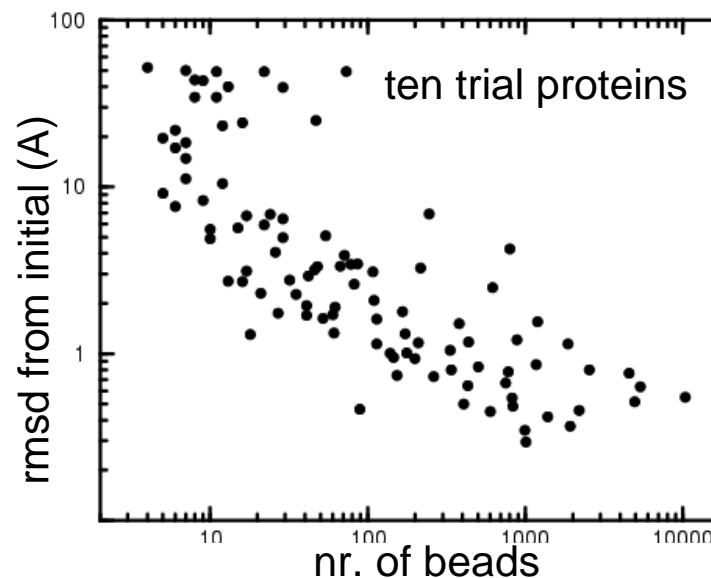
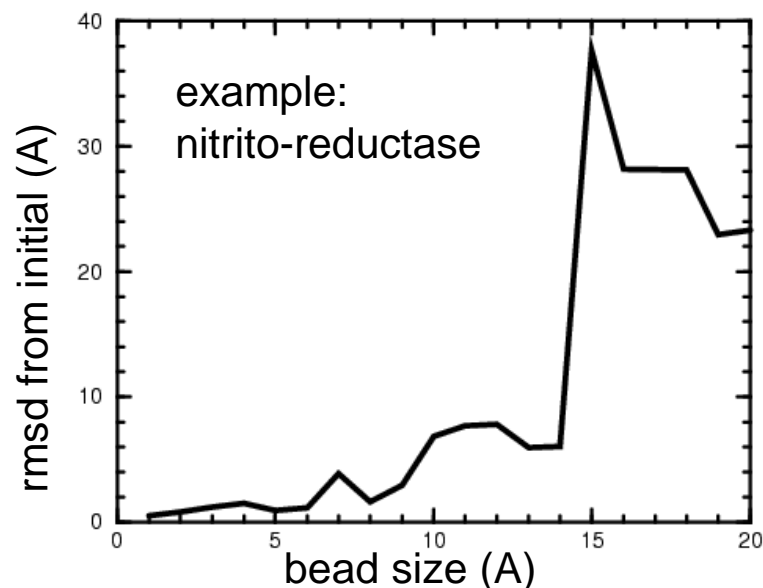


simulated bead models
on a Hexagonal Close-
Packed (HCP) lattice:
“pdb2sax”

Example: Ovalbumin

(Wriggers & Chacon, J. Appl. Cryst., 34:773 (2001))

Accuracy of SAXS Rigid-Body Fitting



- rmsd is stable in lower single digits, until break-down occurs
- ten trial proteins (7cat,1qg3,2cga,1mbn,2nrd,1ova,1xso,1spp,1top,1tub):
 - correct match missed: 0 times
 - unique fit: 7 times (2 times symmetry-related)
 - ambiguous fit (degenerate set of highest-scoring fits): 3 times
 - it turns out that these 3 cases are proteins of sphericity > 0.5 .

Accuracy of SAXS Rigid-Body Fitting

Table 1. Characteristics of simulated SAXS bead models

Protein used for generating bead model	PDB entry	Critical bead size (Å)*	Docking precision (Å)†	Oligomeric symmetry	Degeneracy of best fit‡	Sphericity ζ
Catalase	7cat	16	0.8	4×	4×	0.57
β -4-integrin	1qg3	4	0.8	1×	1×	0.16
Chymotrypsinogen A	2cga	5	2.4	1×	2×	0.66
Myoglobin	1mbn	8	0.8	1×	2×	0.56
Nitrito-reductase	2nrd	15	0.8	3×	6×	0.61
Ovalbumin	1ova	7	0.6	1×	1×	0.48
Spermadhesin	1spp	8	0.8	1×	1×	0.48
Superoxide dismutase	1xso	9	2.7	2×	2×	0.46
Troponin C	1top	9	0.7	1×	1×	0.18
$\alpha\beta$ -tubulin	1tub	11	1.8	1×	1×	0.48

* The value given is the smallest bead radius for which the rms deviation of the docked[§] to the target structure exceeded 10 Å.

† The stated value is the rms deviation of the docked[§] to the target structure averaged for bead radii 1, 2, and 3 Å.

‡ The degeneracy is the number of optimum fits (at sub-critical bead size) that were empirically found to cluster within a narrow numeric range of the optimum score, due to symmetry effects or due to ambiguity of matching.

§ For rmsd evaluations, the fit with the lowest rmsd among any degenerate fits was selected.

Accuracy of SAXS Rigid-Body Fitting

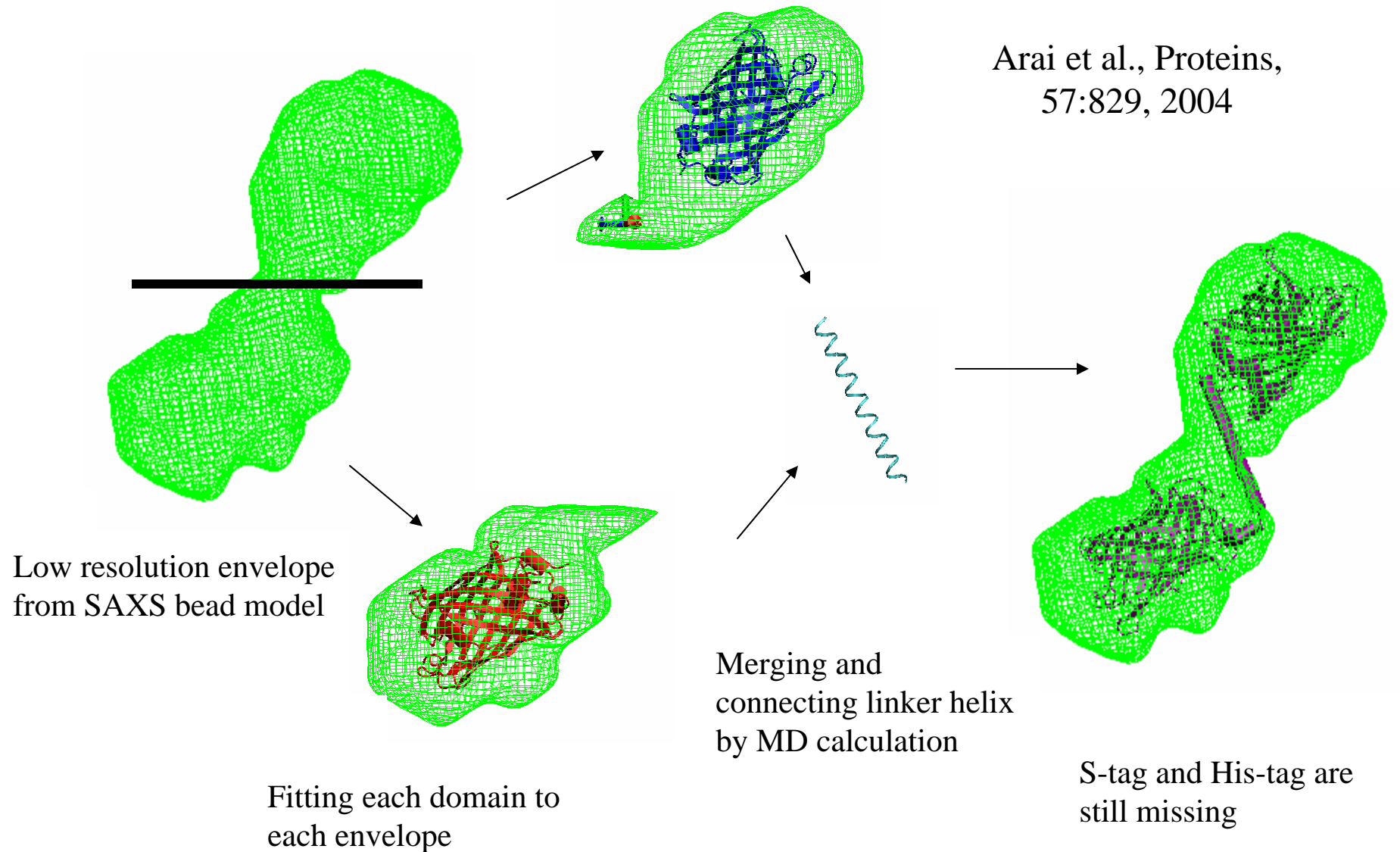
Based on the simulated SAXS trial runs, we can expect that fitting

- does not miss the correct match,
- but on occasion (for globular proteins), the correct match may be part of a number of degenerate highest-scoring fits (need more information).

The accuracy of the docking is on the order of 1Å (or better) for more than 100 beads.

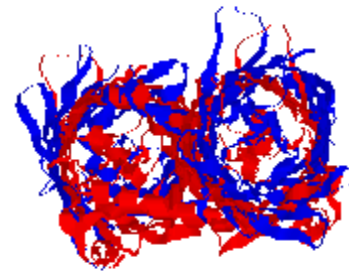
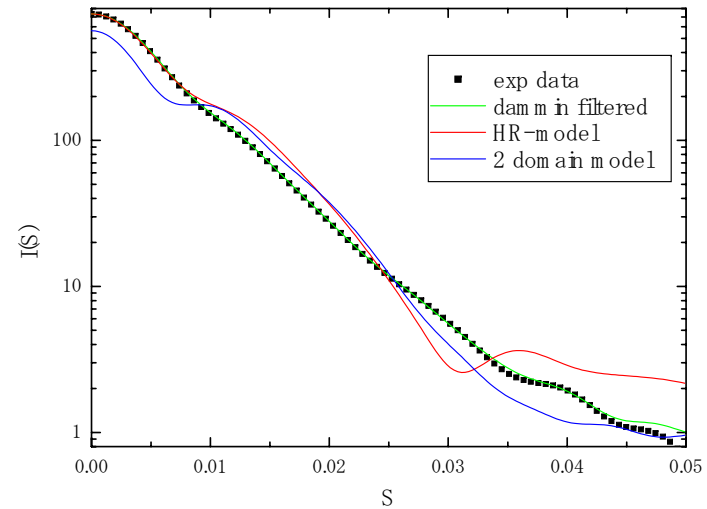
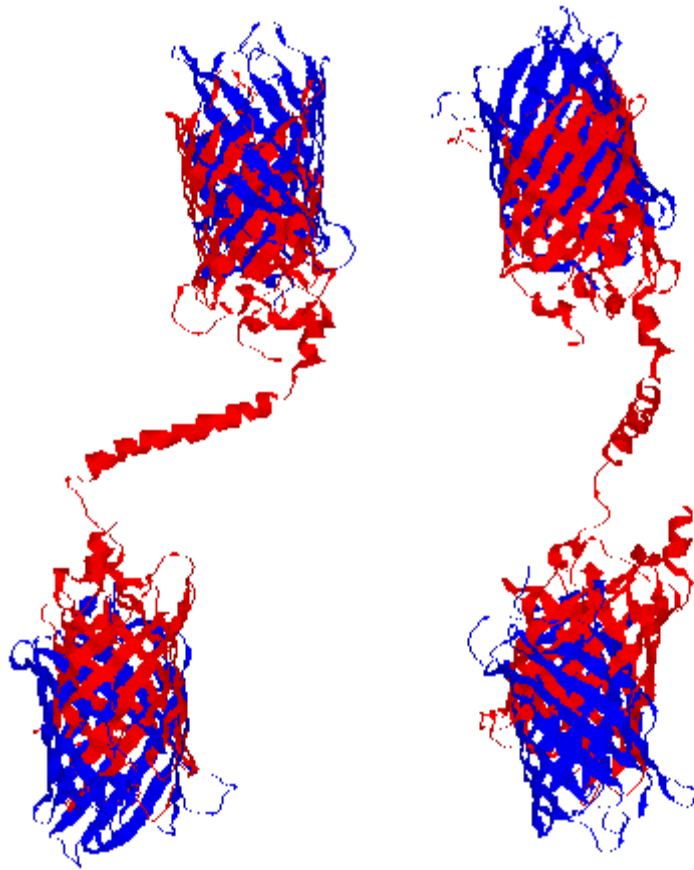
Large Systems: Connecting the Domains

Arai et al., Proteins,
57:829, 2004



© Tetsuro Fujisawa

Real vs. Reciprocal Space Refinement



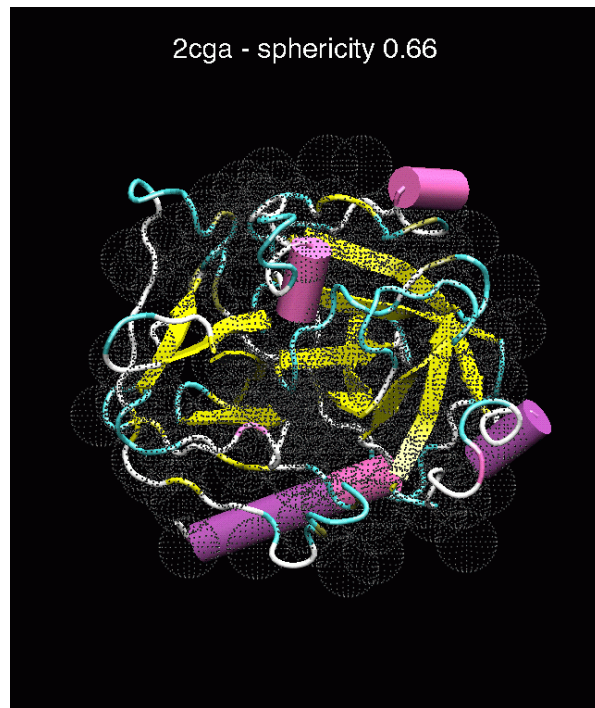
2 domain fitting with
Masha

High resolution model
with Situs

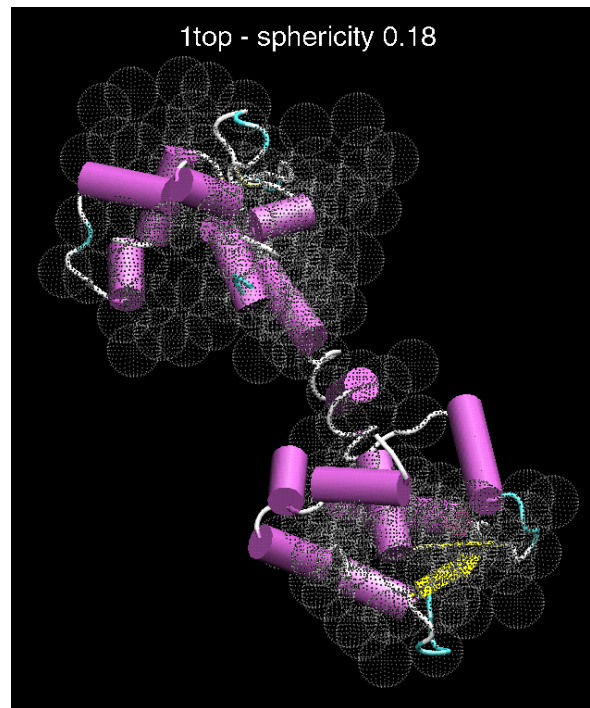
The domain orientation is robust

2001: First SAXS Application of Situs

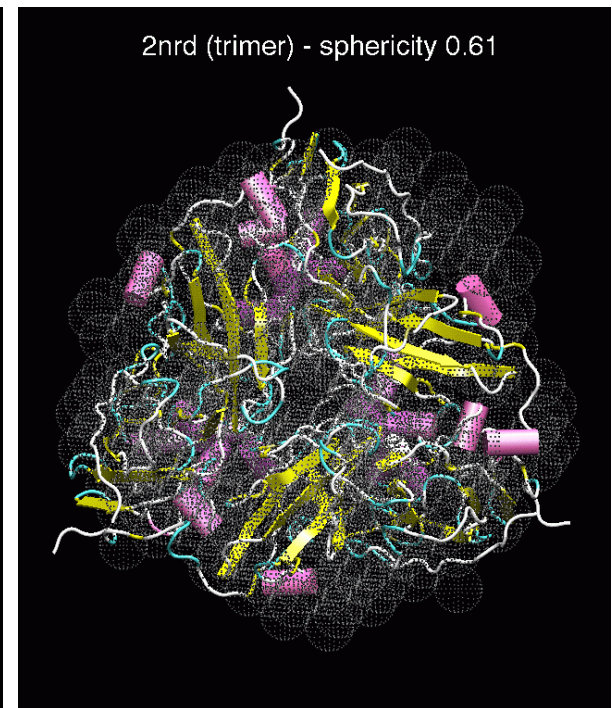
(Wriggers & Chacon, J. Appl. Cryst., 34:773 (2001))



Chymotrypsinogen A



Troponin C



Nitrito-Reductase

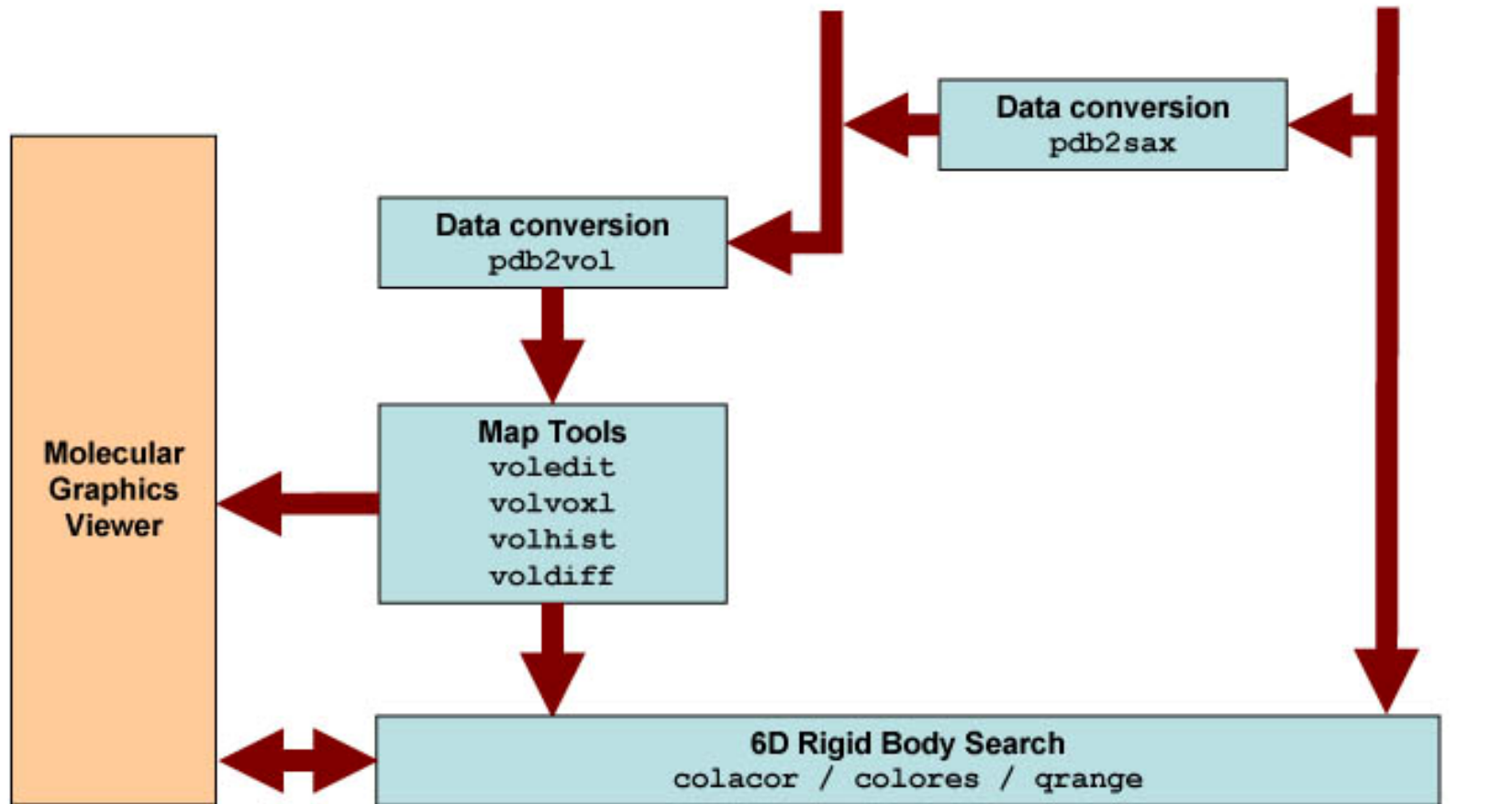
Design (SAXS)

Visualization

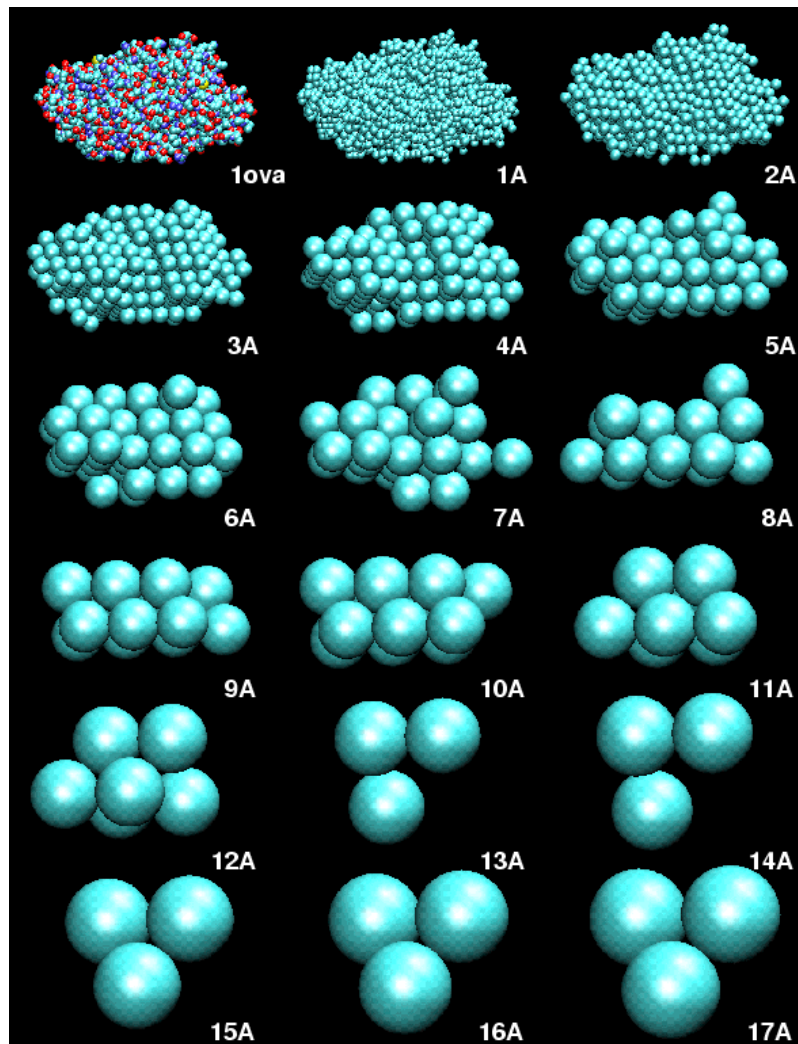
3D Volume
(Situs format)

SAXS Bead Model
(PDB, reconstruction)

Atomic Structure
(PDB)



pdb2sax



simulated bead models
on a Hexagonal Close-
Packed (HCP) lattice

Example: Ovalbumin

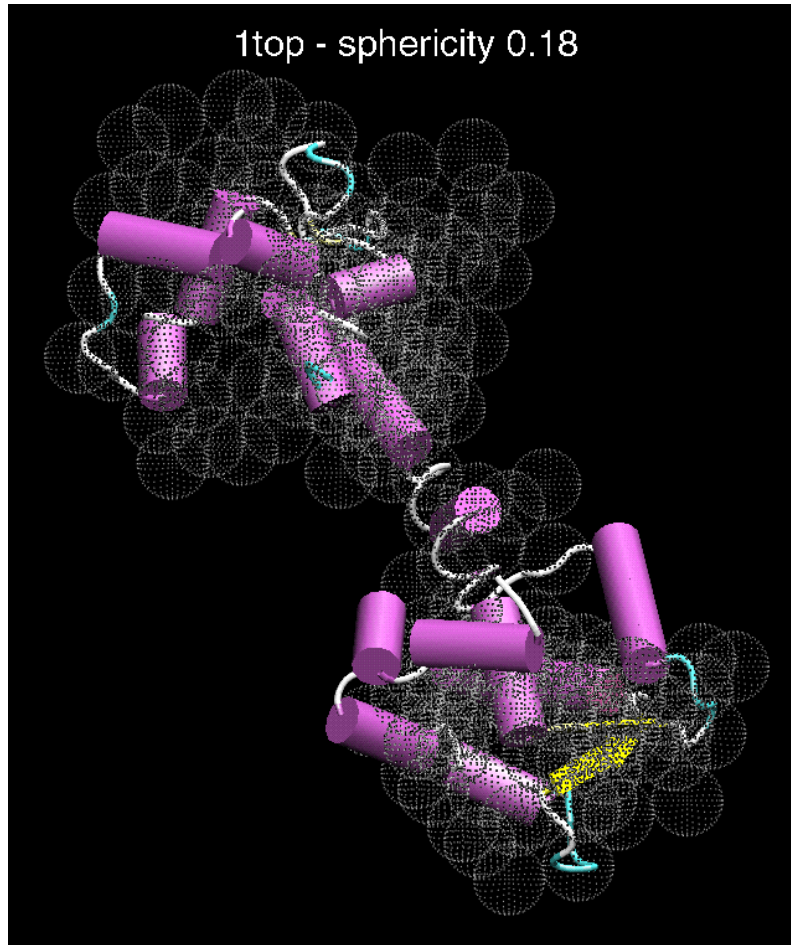
pdb2vol

Convolution with various kernels:
Gaussian, hard sphere, cone, etc

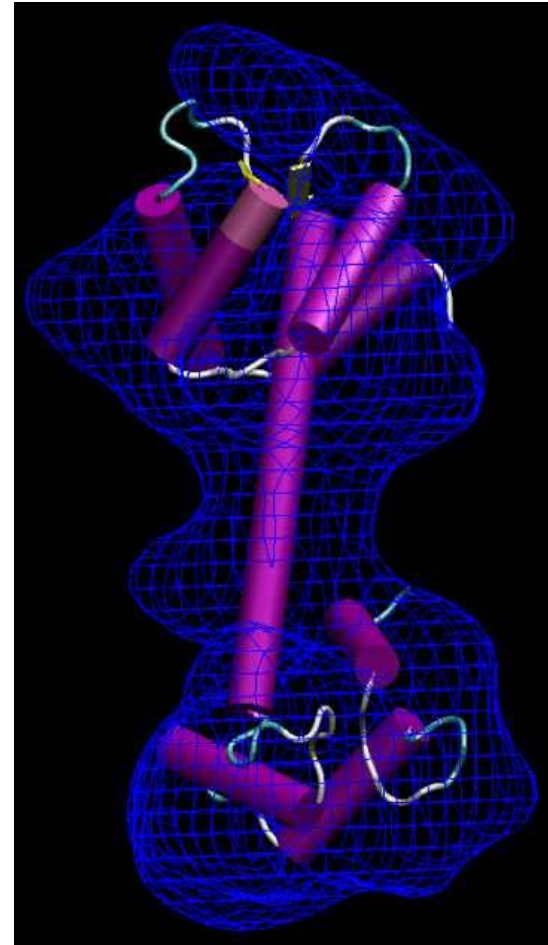
2 uses:

- take SAXS bead model (centers of beads) and create EM style 3D volume map (hard sphere)
- create smooth envelope surrounding beads for visualization (Gaussian)

Visualization



old style: transparent beads



new style: isocontour

Fitting/Refinement

- **colores**: 6D FFT-based rigid-body (slow, but parallelized)
- **colacor**: rigid-body refinement of manual fit (gradient ascent of cross correlation)
- **qrange**: fast rigid-body (based on simulated markers, reduced search space)
- **qpdb + qvol + MD** refinement (X-PLOR): flexible fitting

Acknowledgements

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<http://biomachina.org>

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