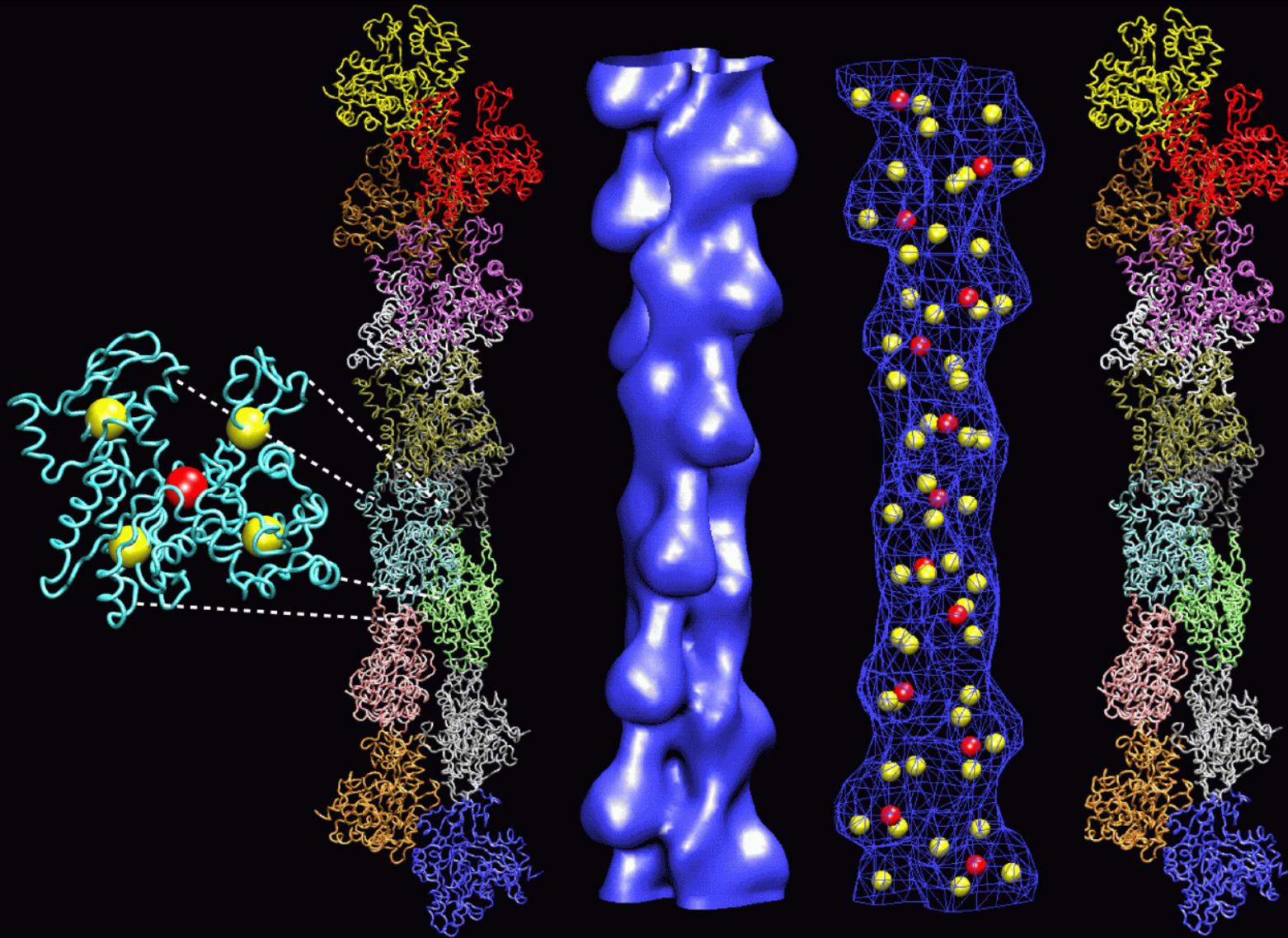


# Flexible Docking

Willy Wriggers

School of Health Information Sciences &  
Institute of Molecular Medicine  
University of Texas – Houston

# “Simulated Markers”



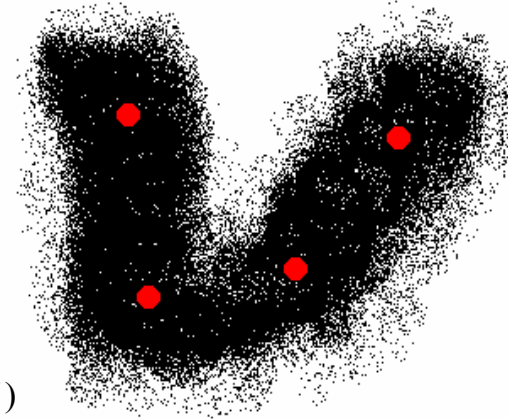
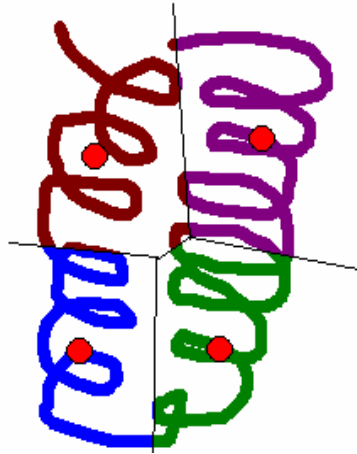
Actin filament: Reconstruction from EM data at 20Å resolution

rmsd: 1.1Å

# Application in Flexible Fitting

Xtal  
structure

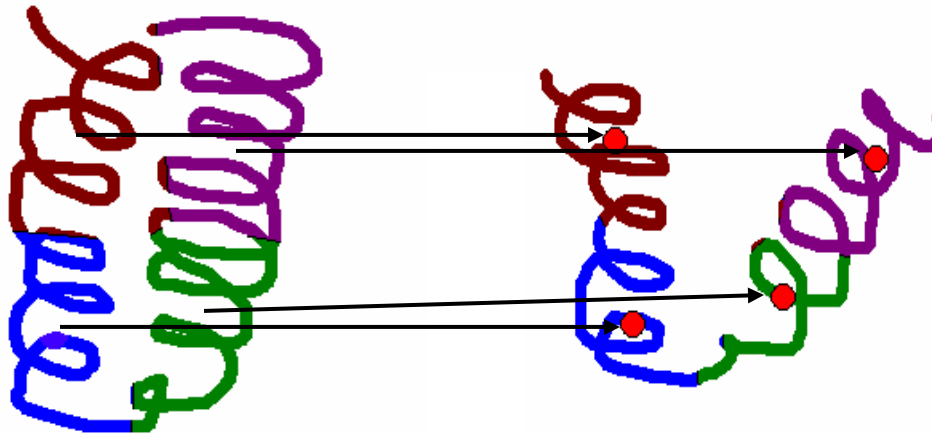
$w_j^{(h)}$



3D EM  
reconstruction

$w_j^{(l)}$

constrain  
centroids



molecular  
dynamics  
simulation

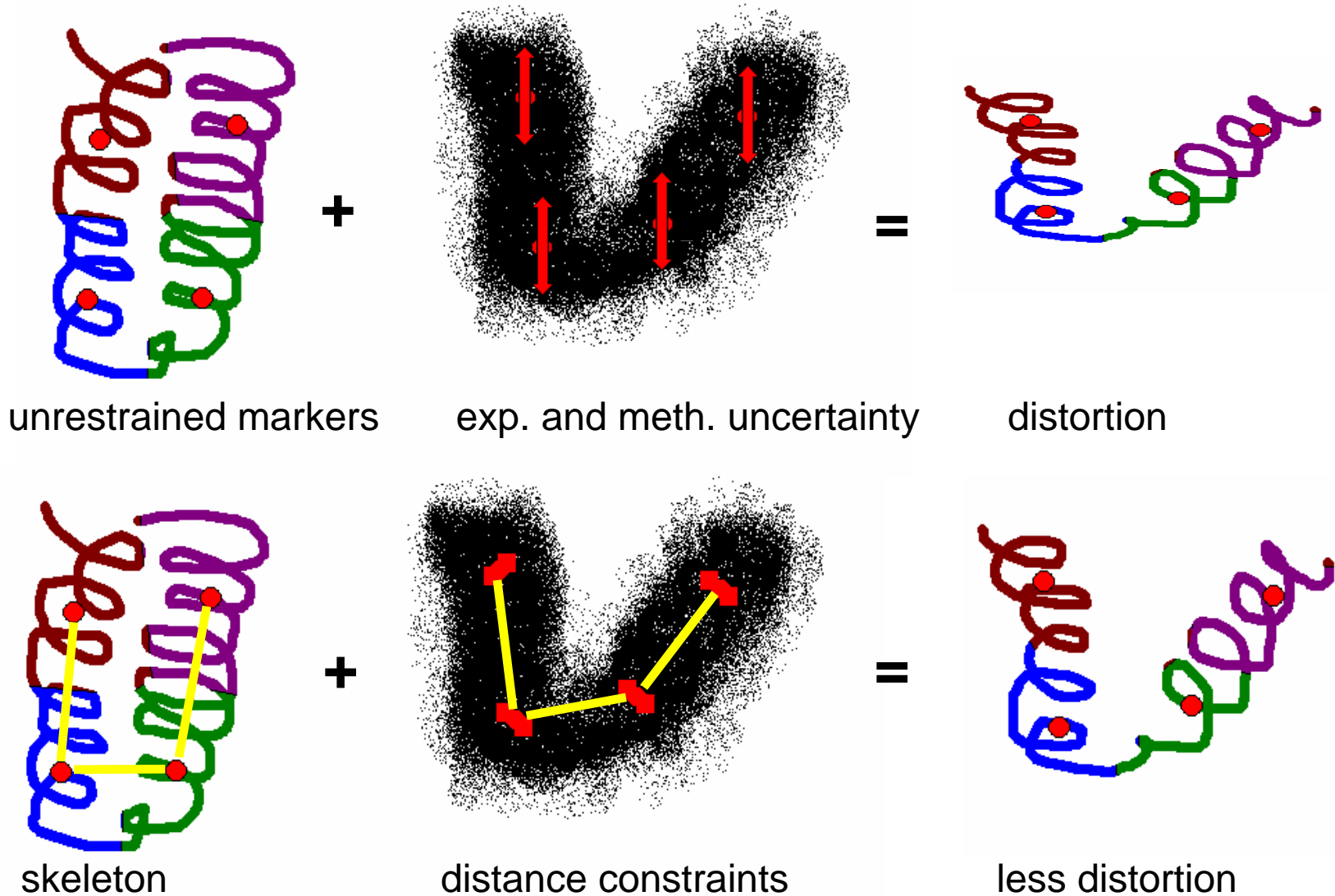
# Stereochemical Quality of Flexible Fitting

The atomic model has many more degrees of freedom than there are independent pieces of information in the EM map. Hence, there is the danger that over fitting distorts the structure

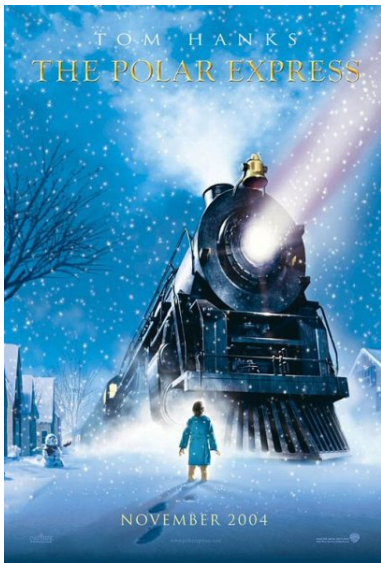
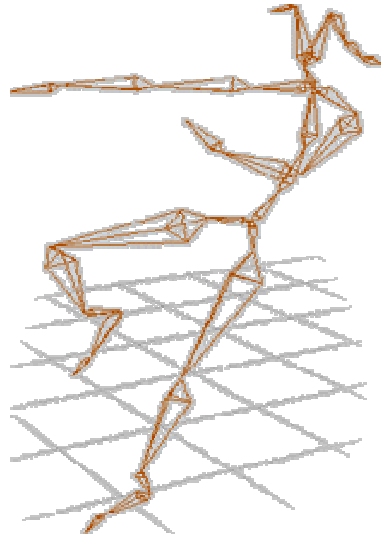
How can over fitting be avoided? Reduce noise by eliminating “inessential” degrees of freedom!...

# Skeletons Limit the Effect of Noise:

freezing inessential degrees of freedom:



# Fitting Skeletons: Motion Capture

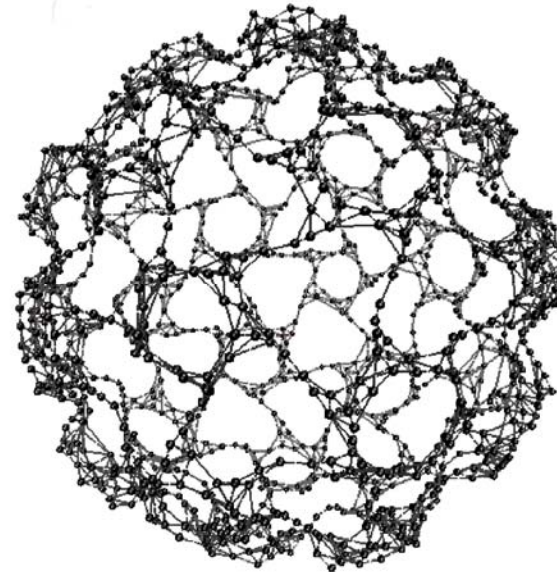
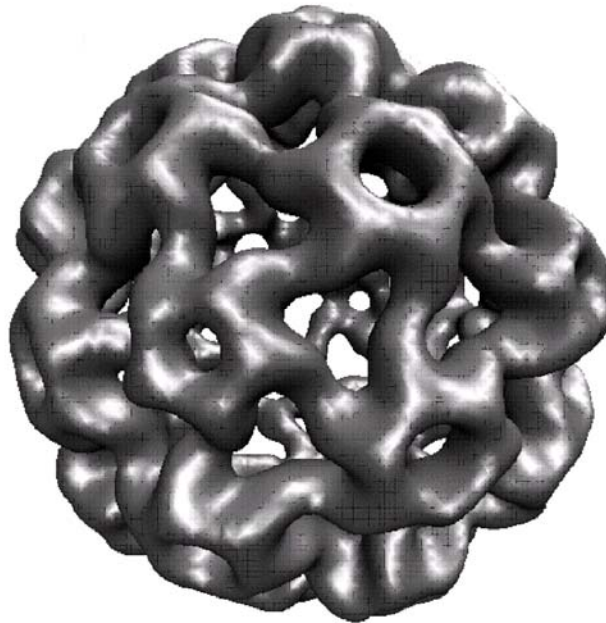


# Motion Capture Network

Topology Representing Neural Network  
(Martinetz and Schulten, 1993)

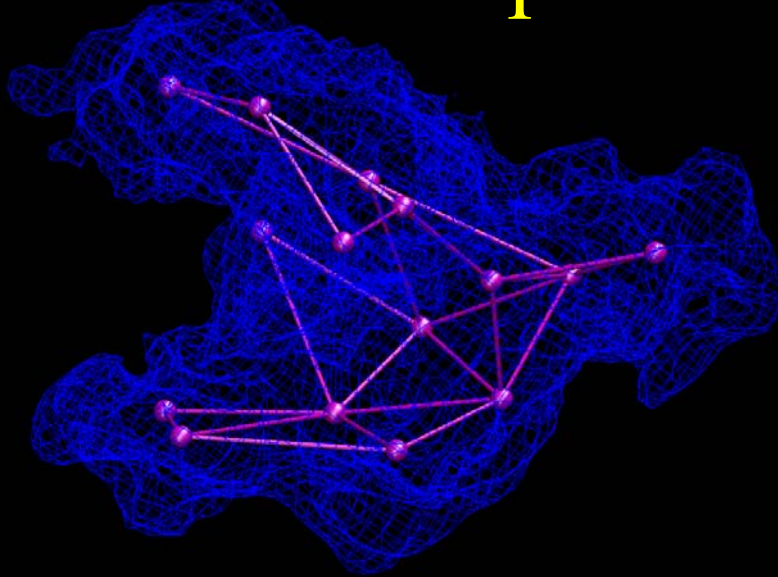
+

SHAKE Distance Constraints  
(van Gunsteren, 1977)

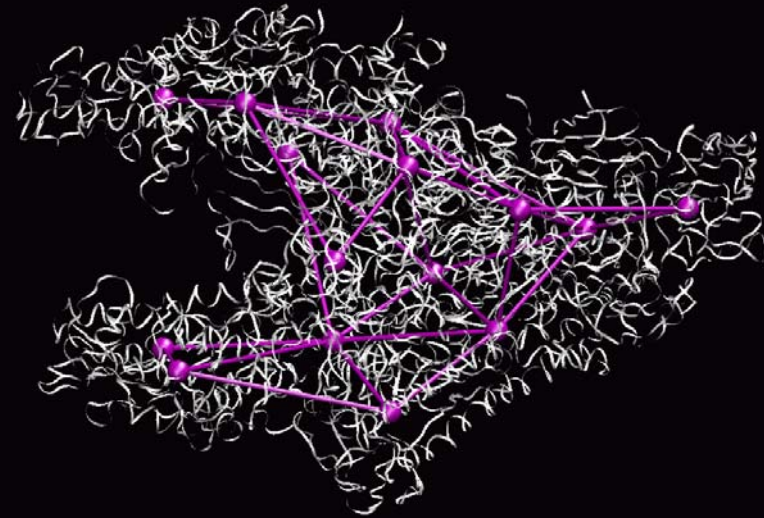


*Neurocomputing (2004) 56:365*

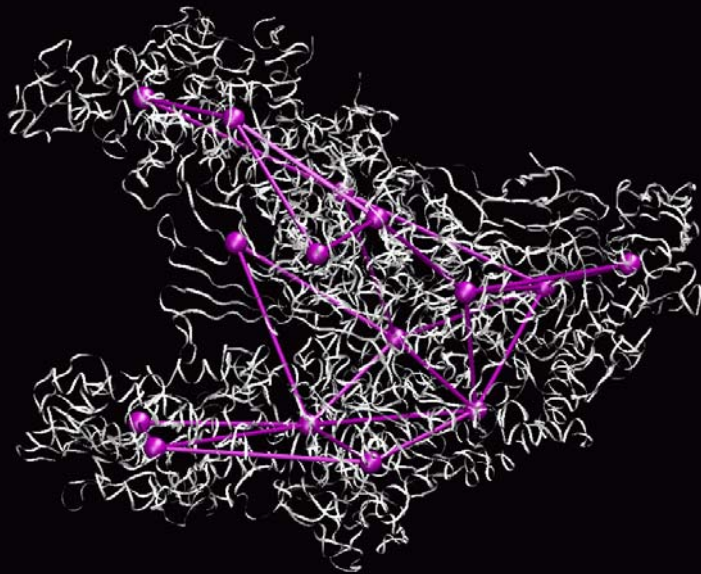
# Motion Capture of RNA Polymerase



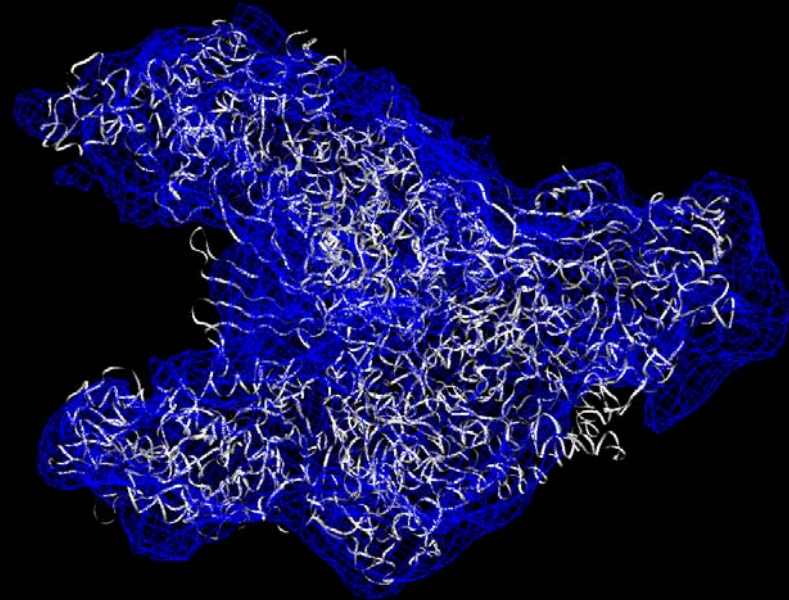
*Taq*-like single molecule map



*Taq* RNAP x-tal structure



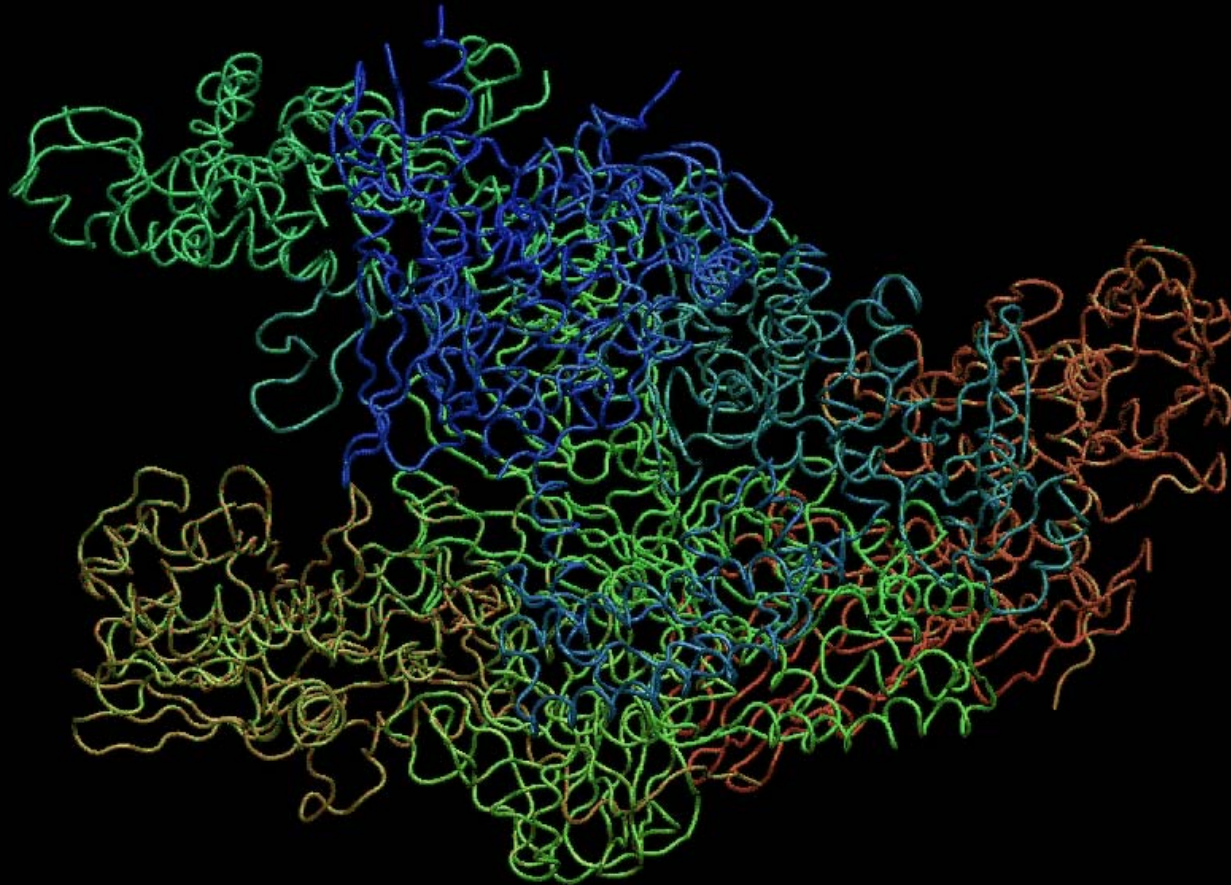
flexible fitting (15 vectors)



final result



# Domain Motions

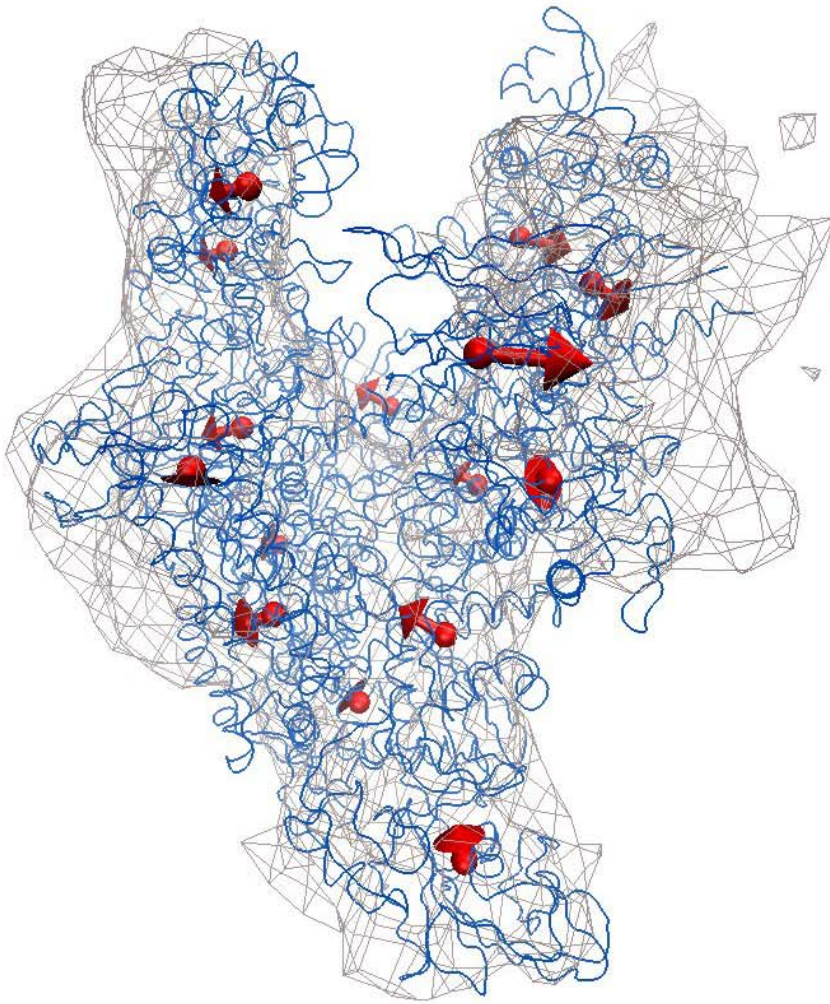


Flexing of the RNAP “jaws” suggests a jaw-closing in presence of DNA

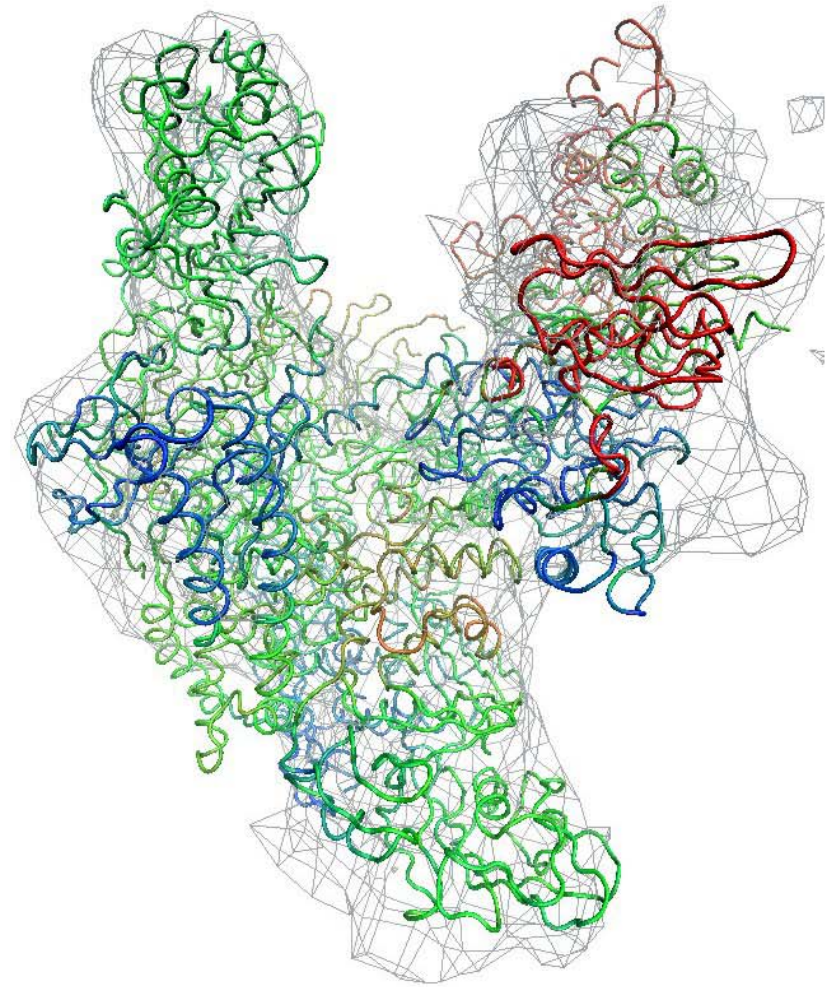
*PNAS* (2002) 99:4296

*Cell* (2003) 114:335

# What Information is Used?



Displacements



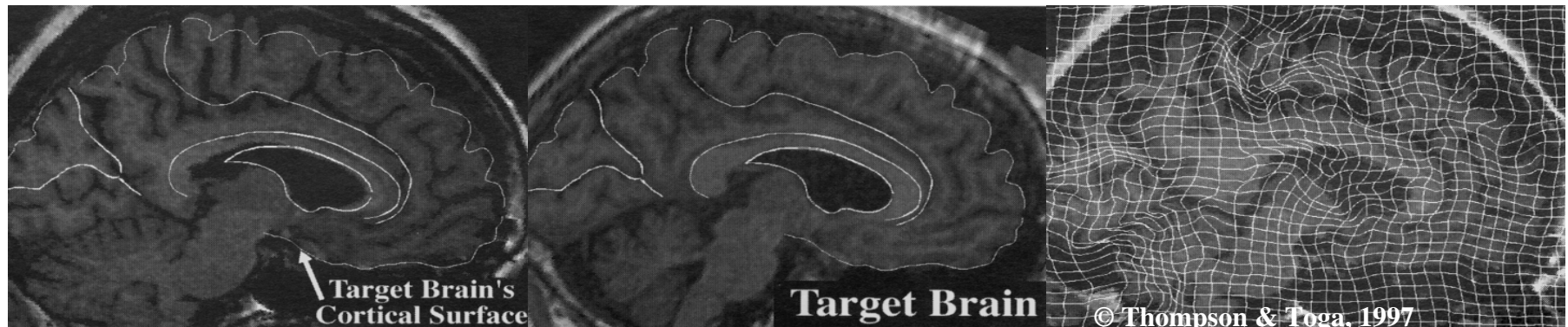
Molecular Dynamics

# Molecular Dynamics vs. Interpolation

MD simulation requires an expert user and hours of preparation. We know a sparse estimation of the displacement field at markers. Can we extend the sparse estimate to the full space by an inexpensive interpolation?

## Interpolation Pros:

- Ease of use / implementation
- Detailed mass rearrangement plan.
- Linear or nonlinear registration of features
- Used in neuroscience and machine vision:



# (i) Piecewise-Linear Inter- / Extrapolation

For each **probe position** find 4 closest vectors.

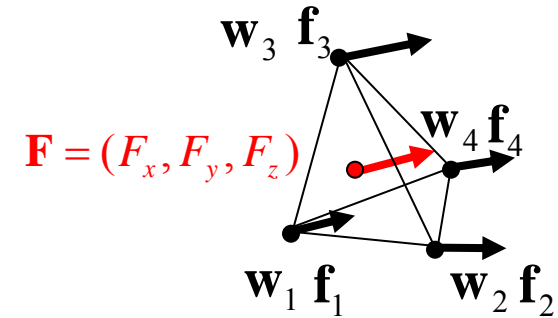
Ansatz:  $F_x(x, y, z) = ax + by + cz + d$

$$F_x(\mathbf{w}_1) = f_{1,x},$$

$$F_x(\mathbf{w}_2) = f_{2,x},$$

$$F_x(\mathbf{w}_3) = f_{3,x},$$

$$F_x(\mathbf{w}_4) = f_{4,x} \quad (\text{similar for } F_y, F_z).$$



Cramer's rule:

$$a = \frac{\begin{vmatrix} f_{1,x} & w_{1,y} & w_{1,z} & 1 \\ f_{2,x} & w_{2,y} & w_{2,z} & 1 \\ f_{3,x} & w_{3,y} & w_{3,z} & 1 \\ f_{4,x} & w_{4,y} & w_{4,z} & 1 \end{vmatrix}}{D}, \quad b = \frac{\begin{vmatrix} w_{1,x} & f_{1,y} & w_{1,z} & 1 \\ w_{2,x} & f_{2,y} & w_{2,z} & 1 \\ w_{3,x} & f_{3,y} & w_{3,z} & 1 \\ w_{4,x} & f_{4,y} & w_{4,z} & 1 \end{vmatrix}}{D}, \quad \dots, \quad D = \begin{vmatrix} w_{1,x} & w_{1,y} & w_{1,z} & 1 \\ w_{2,x} & w_{2,y} & w_{2,z} & 1 \\ w_{3,x} & w_{3,y} & w_{3,z} & 1 \\ w_{4,x} & w_{4,y} & w_{4,z} & 1 \end{vmatrix}$$

## (ii) Non-Linear Kernel Interpolation

Consider all  $k$  vectors and interpolation kernel function  $U(r)$ .

Ansatz:

$$F_x(x, y, z) = a_1 + a_x x + a_y y + a_z z + \sum_{k=1}^k b_i \cdot U(|\mathbf{w}_i - (x, y, z)|)$$

$$F_x(\mathbf{w}_i) = f_{i,x}, \quad \forall i \quad (\text{similar for } F_y, F_z).$$

Solve :

$$\mathbf{L}^{-1}(f_{1,x}, \dots, f_{k,x}, 0, 0, 0, 0) = (b_1, \dots, b_k, a_1, a_x, a_y, a_z)^T,$$

$$\text{where } \mathbf{L} = \left( \begin{array}{c|c} \mathbf{P} & \mathbf{Q} \\ \hline \mathbf{Q}^T & \mathbf{0} \end{array} \right), \quad \mathbf{Q} = \begin{pmatrix} 1 & w_{1,x} & w_{1,y} & w_{1,z} \\ \dots & \dots & \dots & \dots \\ 1 & w_{k,x} & w_{k,y} & w_{k,z} \end{pmatrix}, \quad k \times 4,$$

$$\mathbf{P} = \begin{pmatrix} 0 & U(w_{12}) & \dots & U(w_{1k}) \\ U(w_{21}) & 0 & \dots & U(w_{2k}) \\ \dots & \dots & \dots & \dots \\ U(w_{k1}) & U(w_{k2}) & \dots & 0 \end{pmatrix}, \quad k \times k.$$

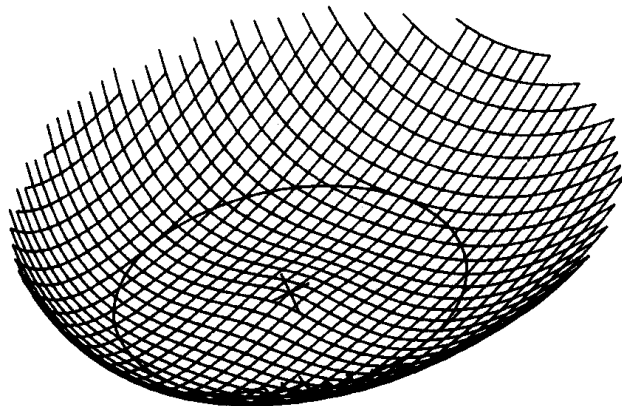
# Bookstein “Thin-Plate” Splines

- kernel function  $U(r)$  is principal solution of **biharmonic equation** that arises in elasticity theory of thin plates:

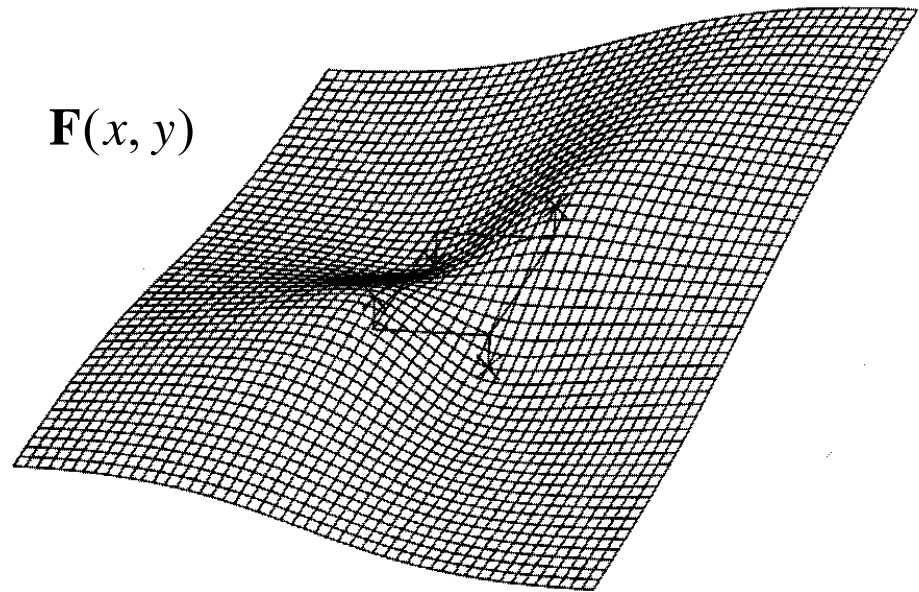
$$\Delta^2 U(r) = \nabla^4 U(r) = \delta(r).$$

- variational principle:  $U(r)$  minimizes the bending energy (not shown).
- 1D:  $U(r) = |r^3|$  (cubic spline)
- 2D:  $U(r) = r^2 \log r^2$
- 3D:  $U(r) = |r|$

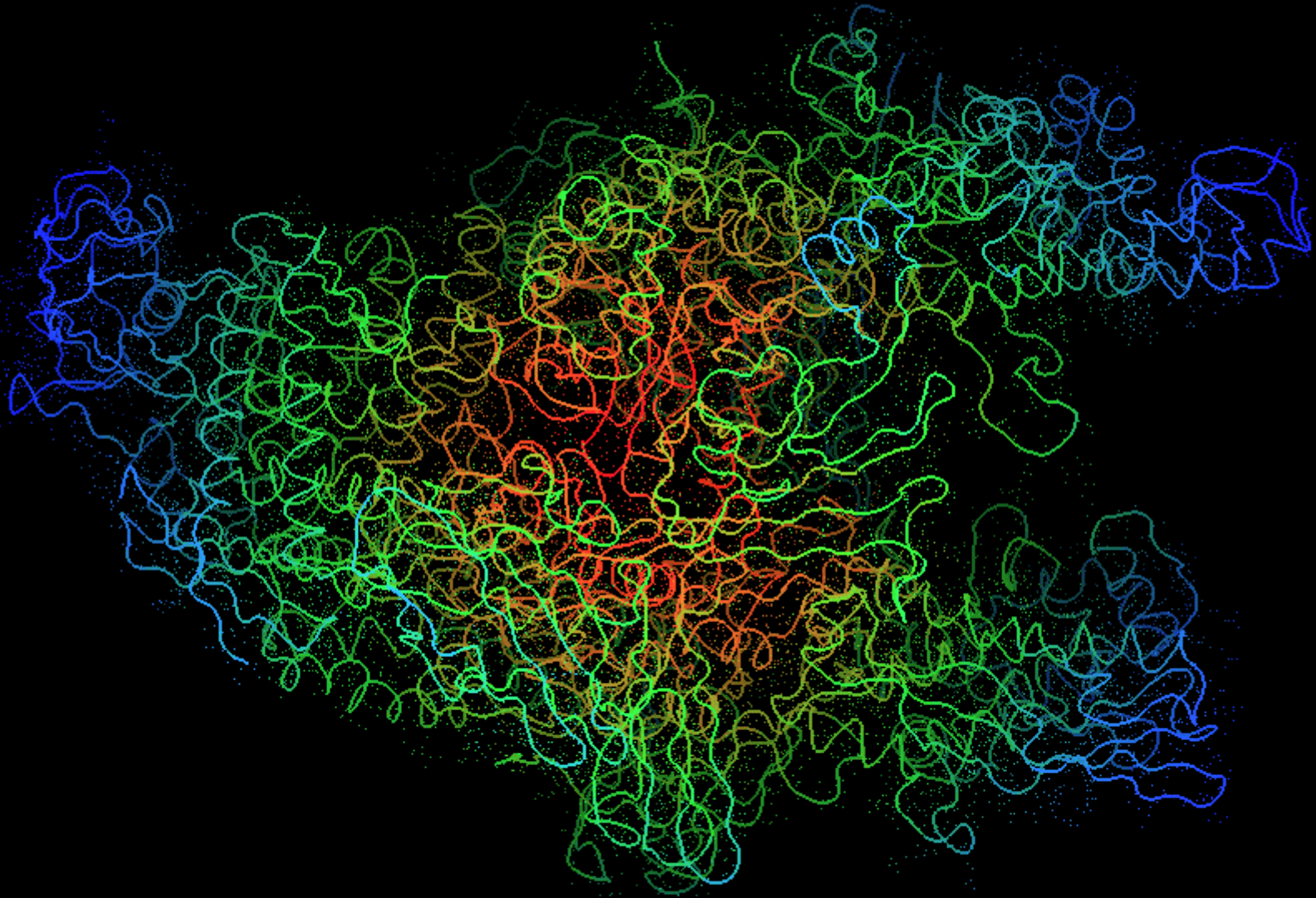
2D:  $U(r)$



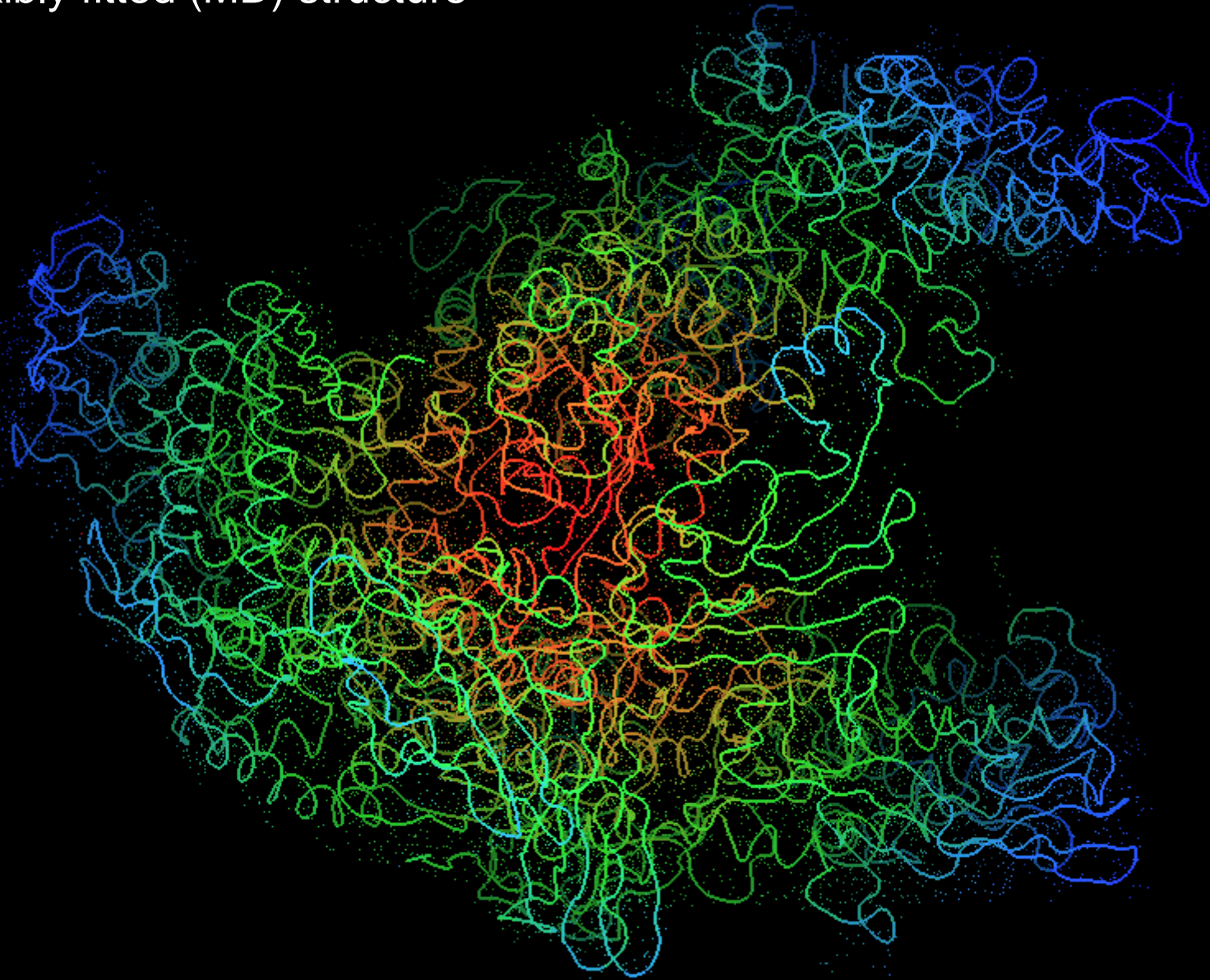
$\mathbf{F}(x, y)$



*Taq* RNAP x-tal structure

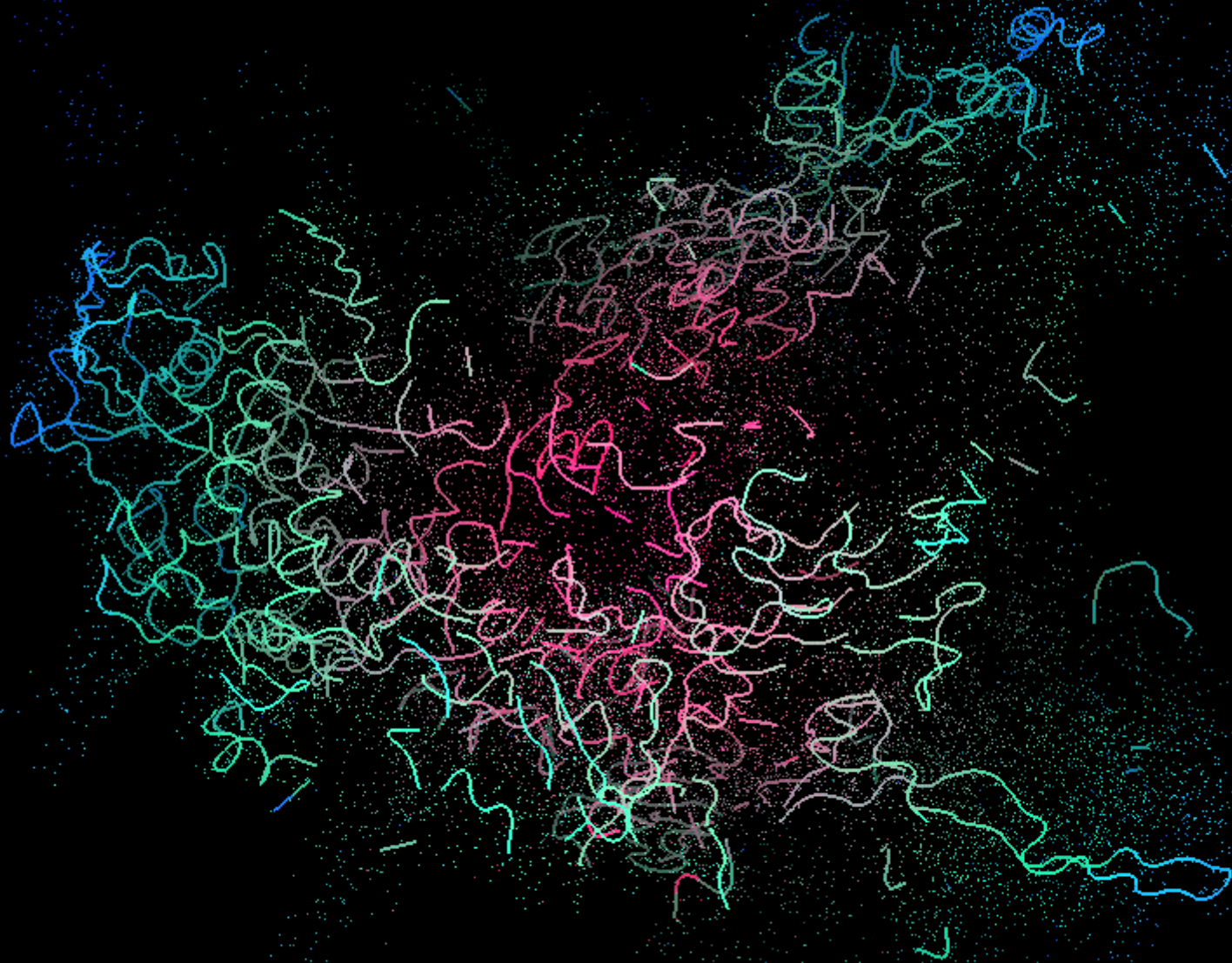


Flexibly fitted (MD) structure

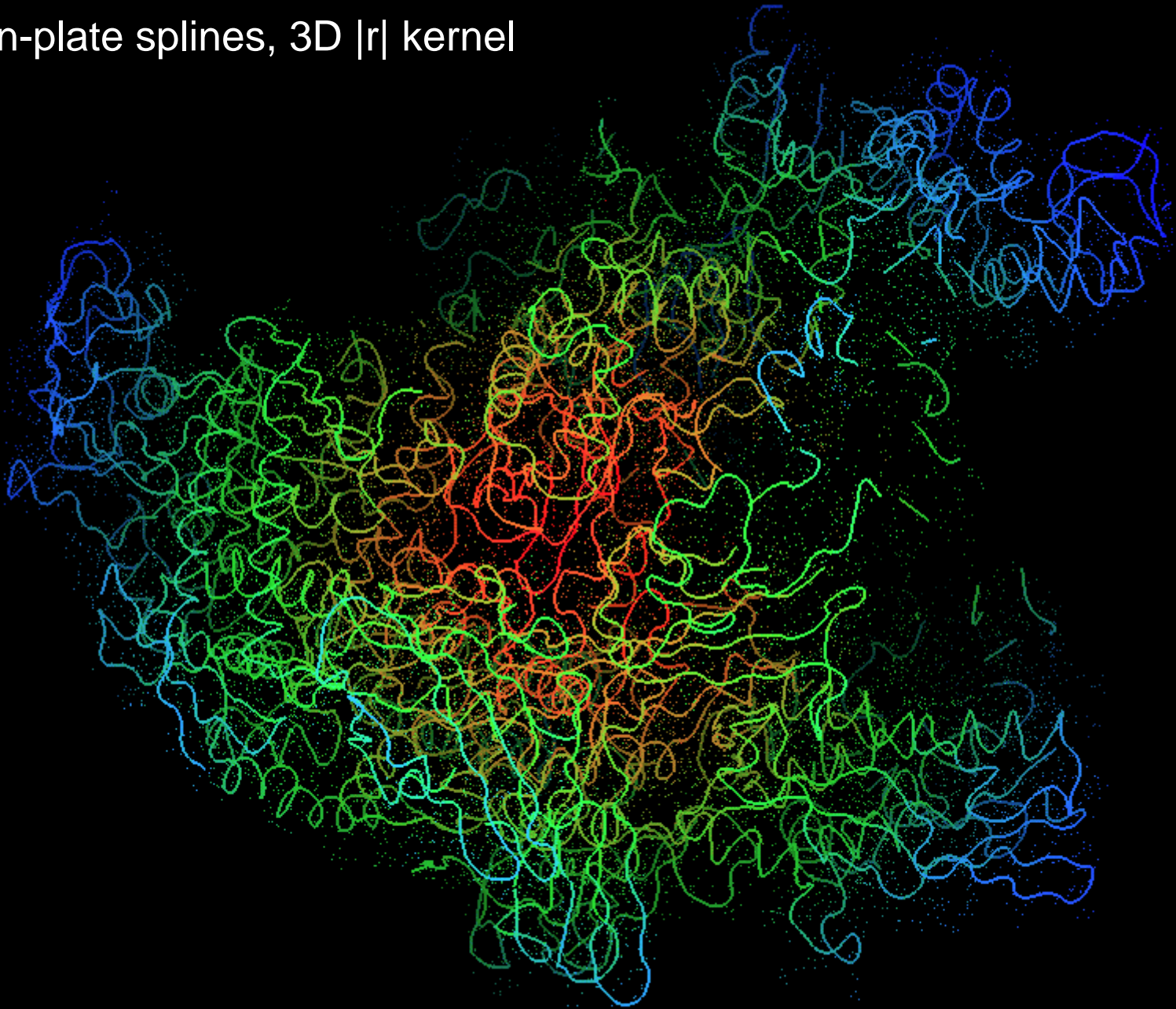




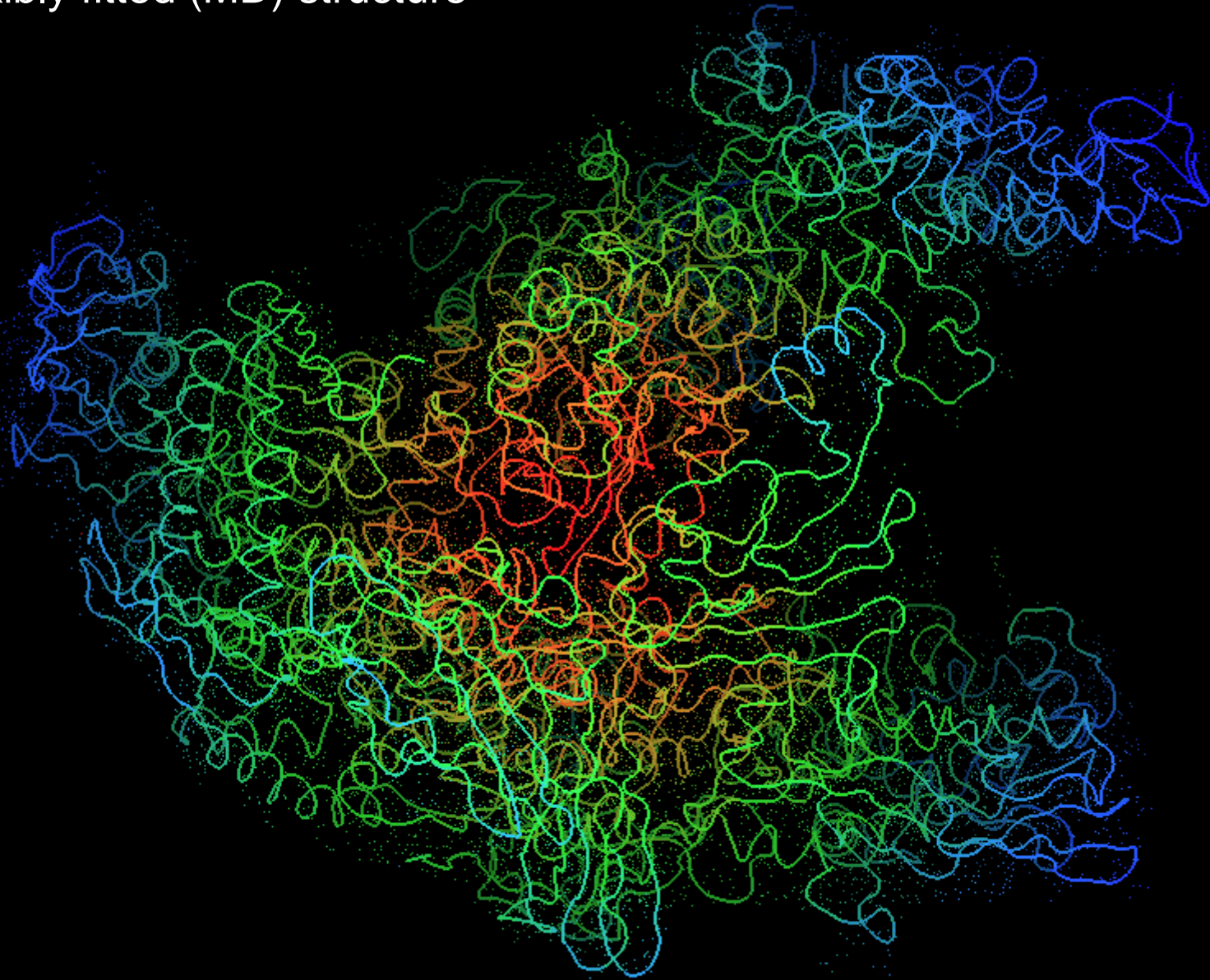
# Piecewise-linear inter- / extrapolation



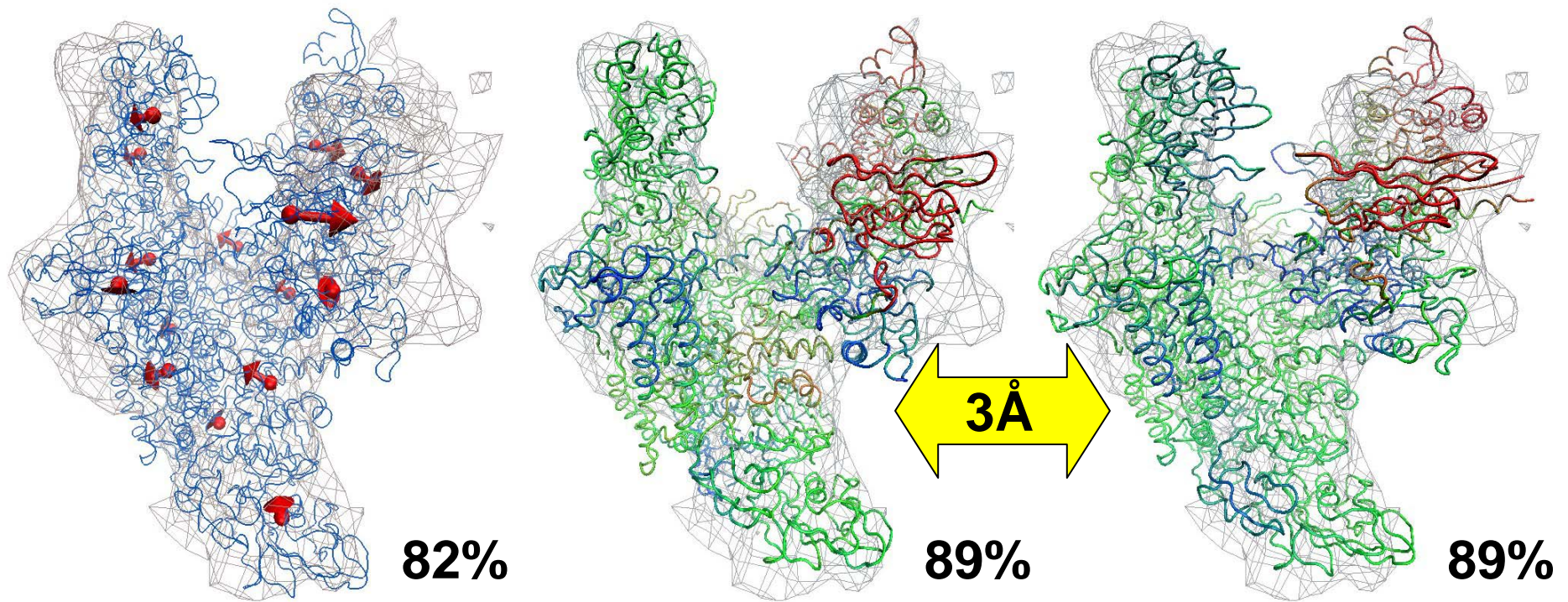
Thin-plate splines, 3D  $|r|$  kernel



Flexibly fitted (MD) structure



# MD vs. Thin Plate Splines



Displacements

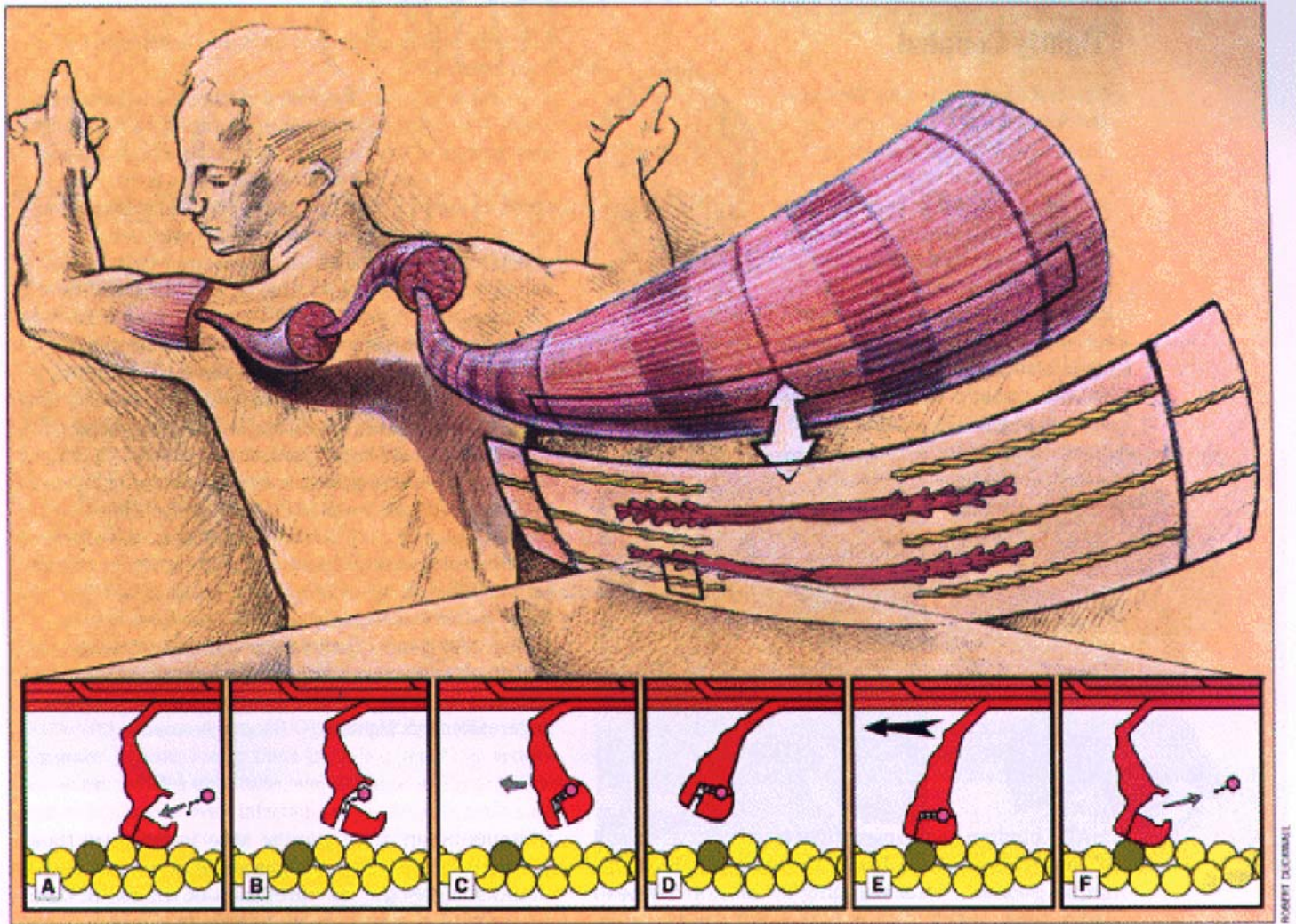
Molecular Dynamics

Thin-Plate Splines

How do we know MD is really better?

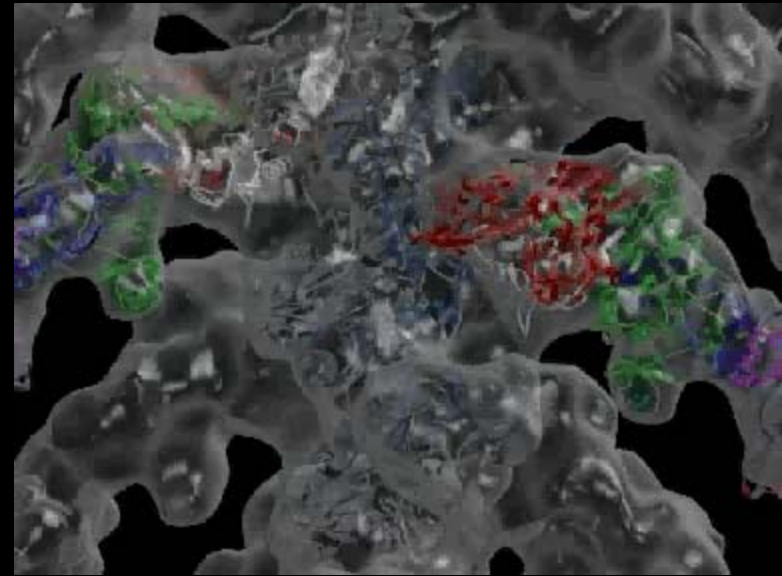
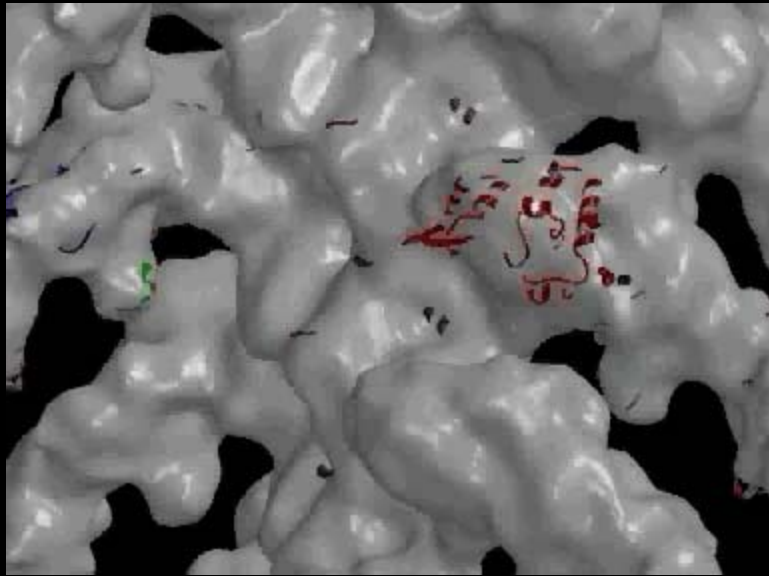
*Structure* (2004) 12:1

# Validation Example: Muscle Contraction



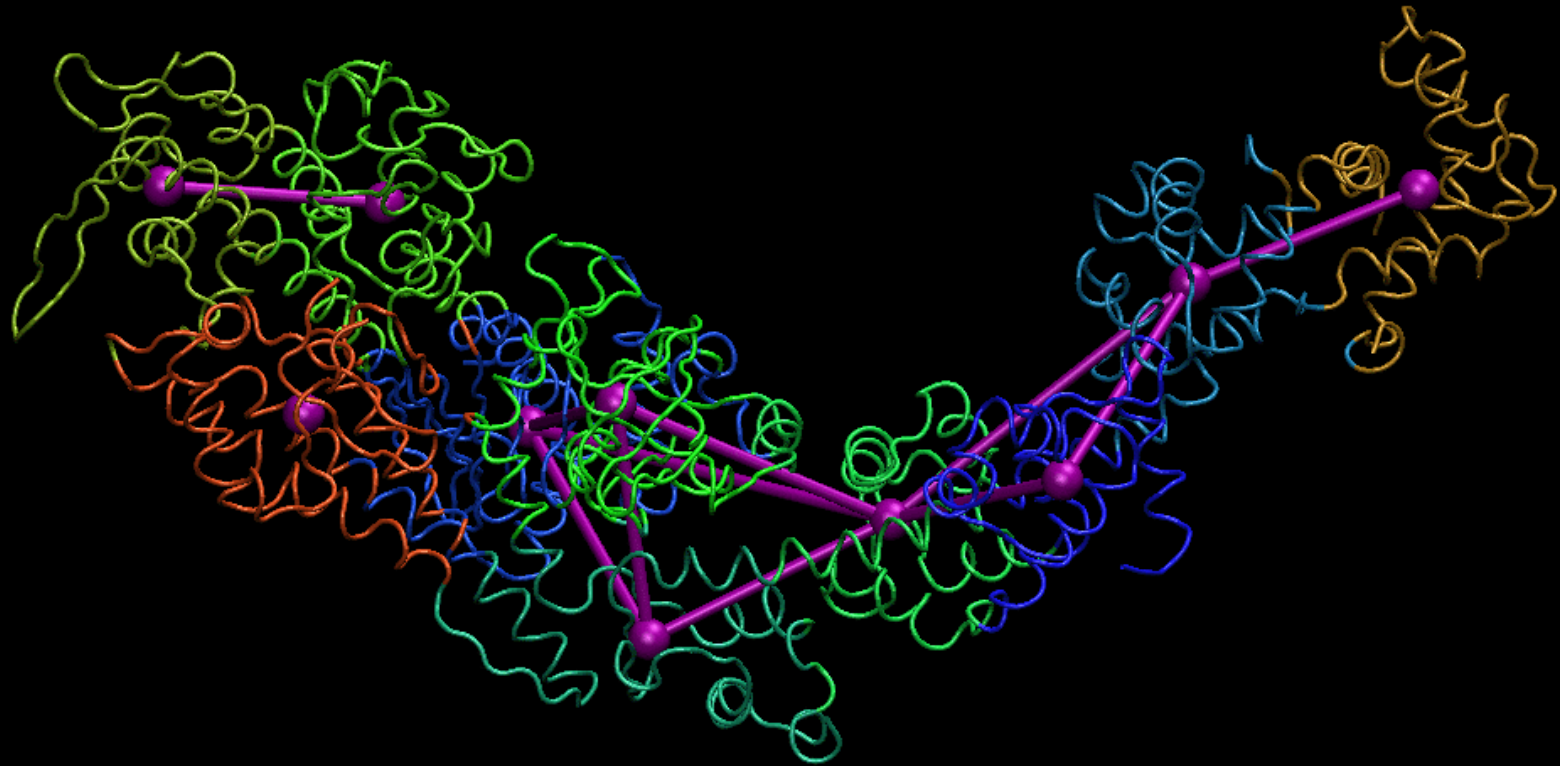
A Hierarchy of Muscle Structure, J. NIH Res. 1993

# Acto-Myosin (II) Complex at 14Å

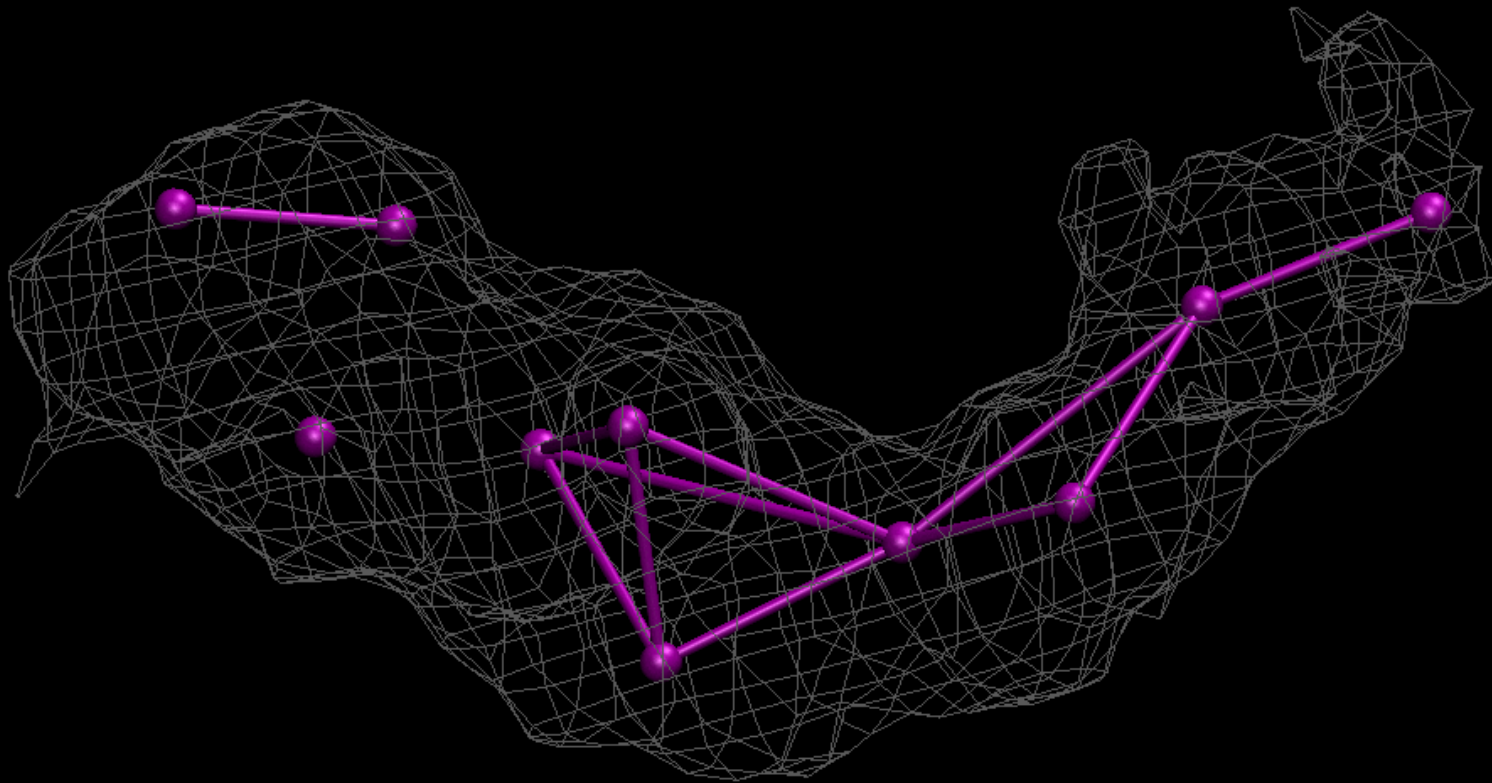


R. Schröder et al., *Nature* (2003) 425:423

# Flexing of Myosin II

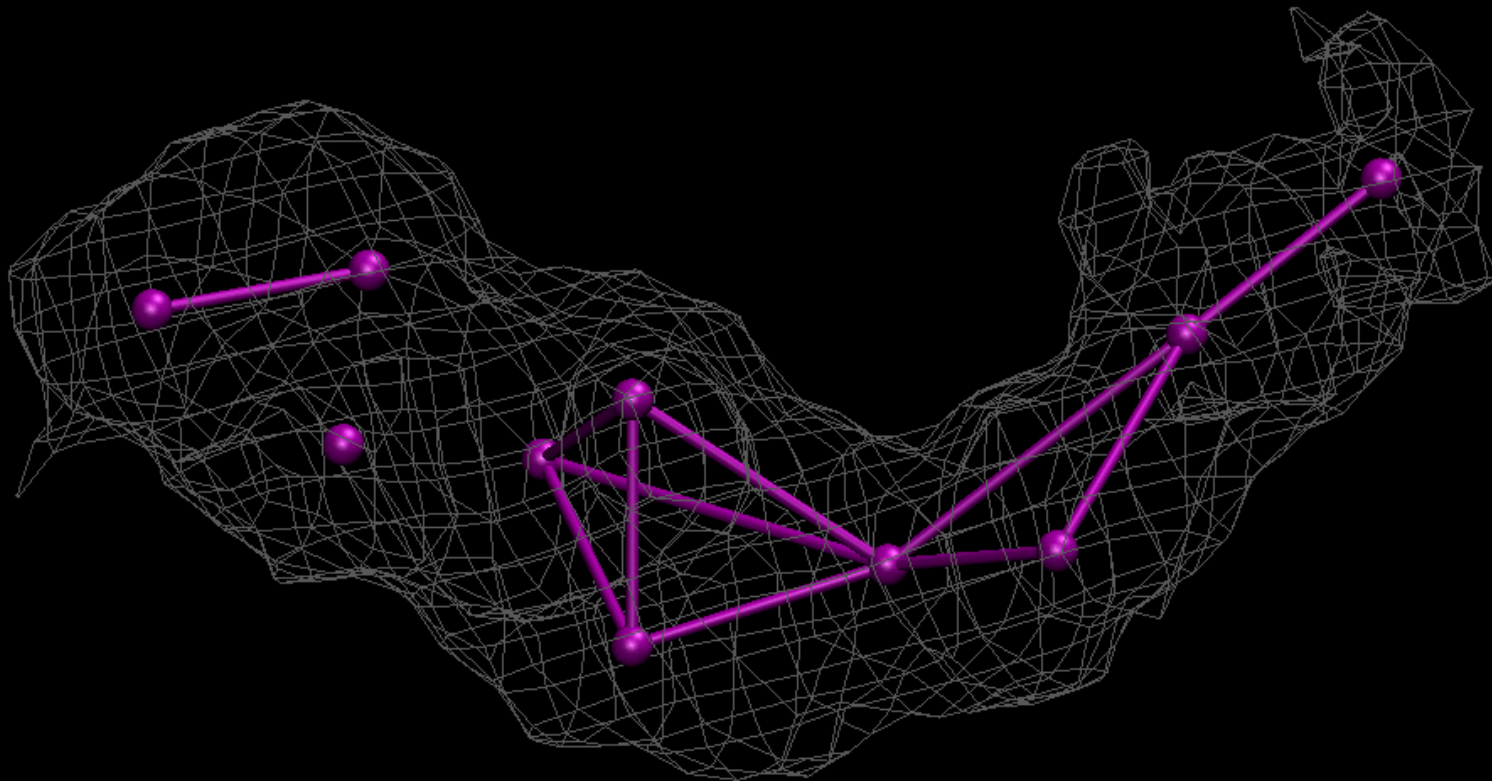


# Flexing of Myosin II

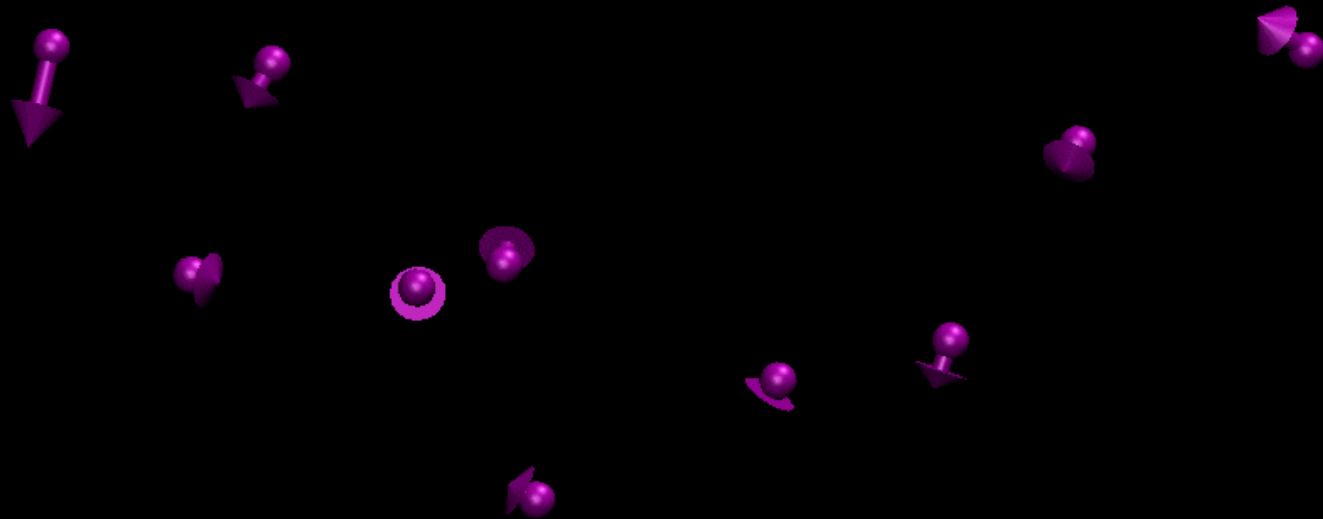




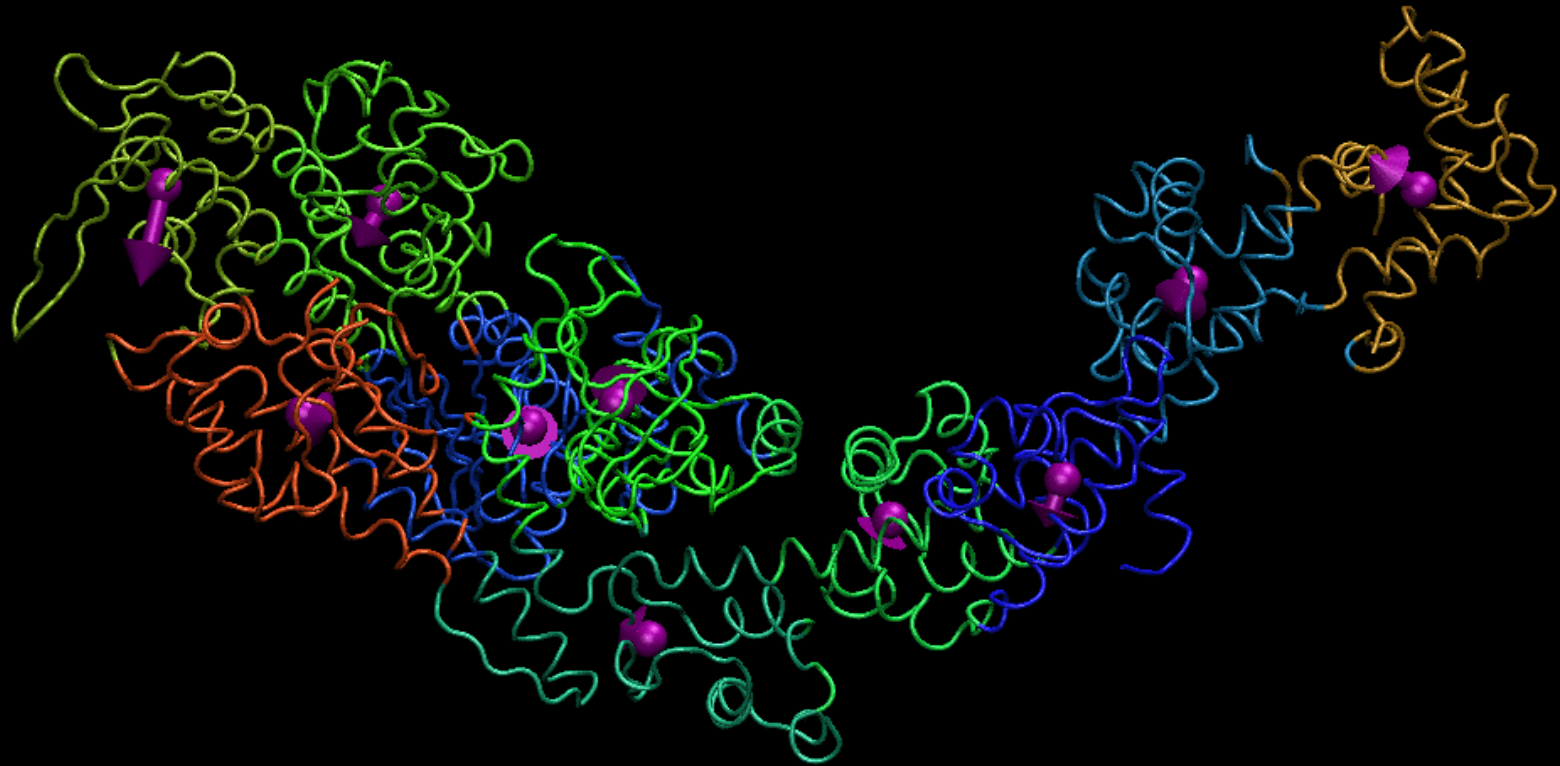
# Flexing of Myosin II



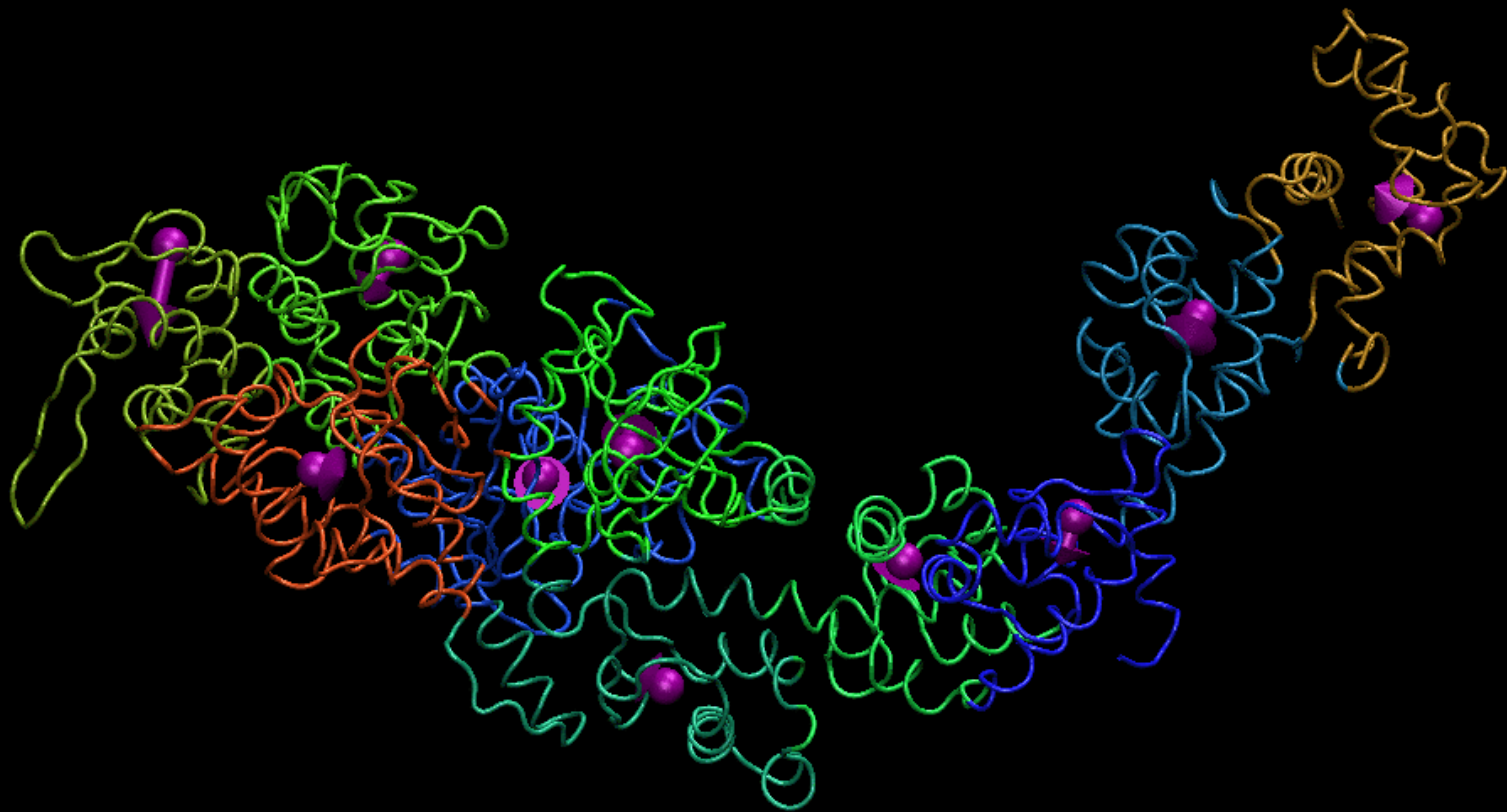
# Flexing of Myosin II



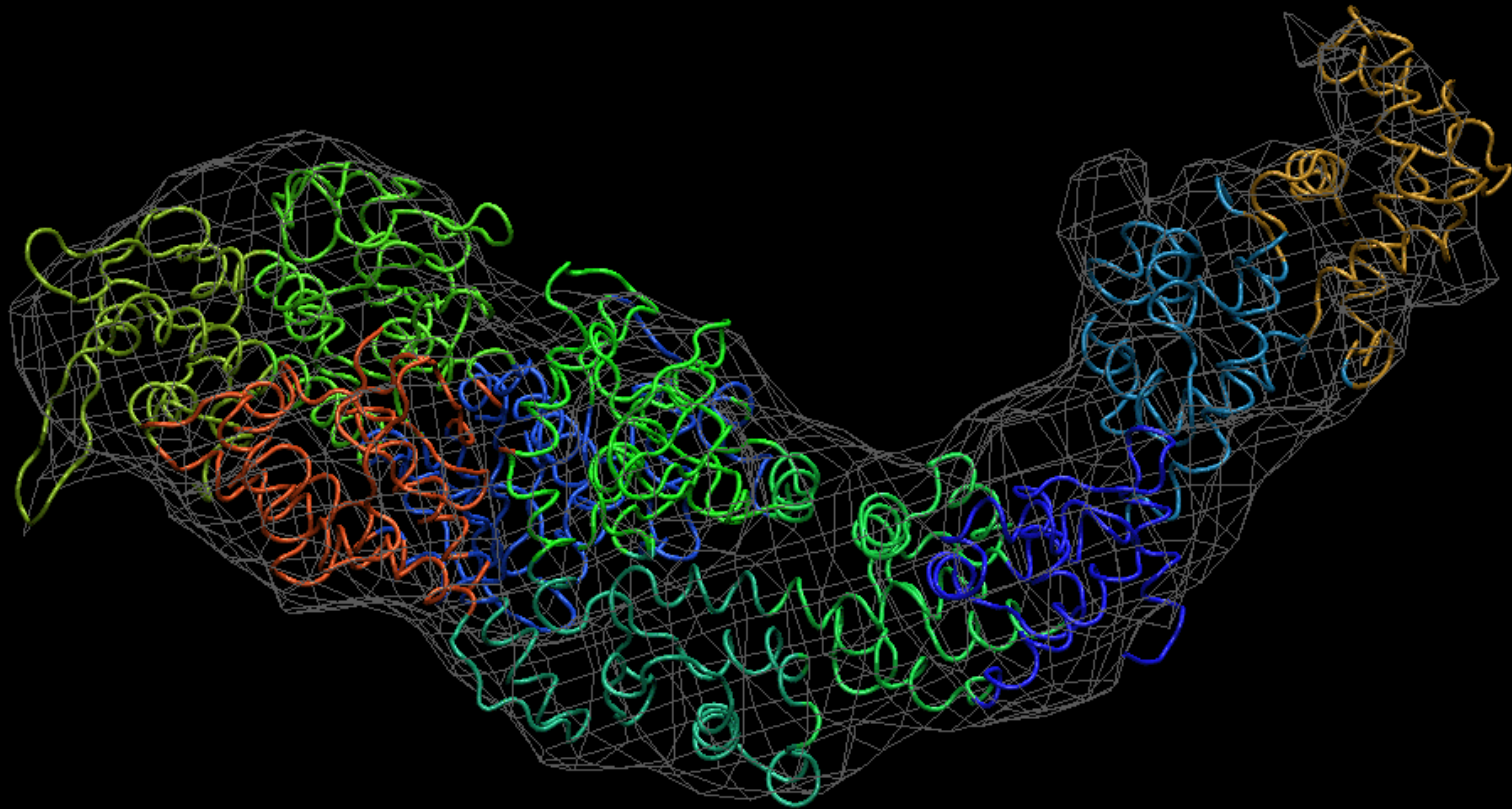
# Flexing of Myosin II



# Flexing of Myosin II



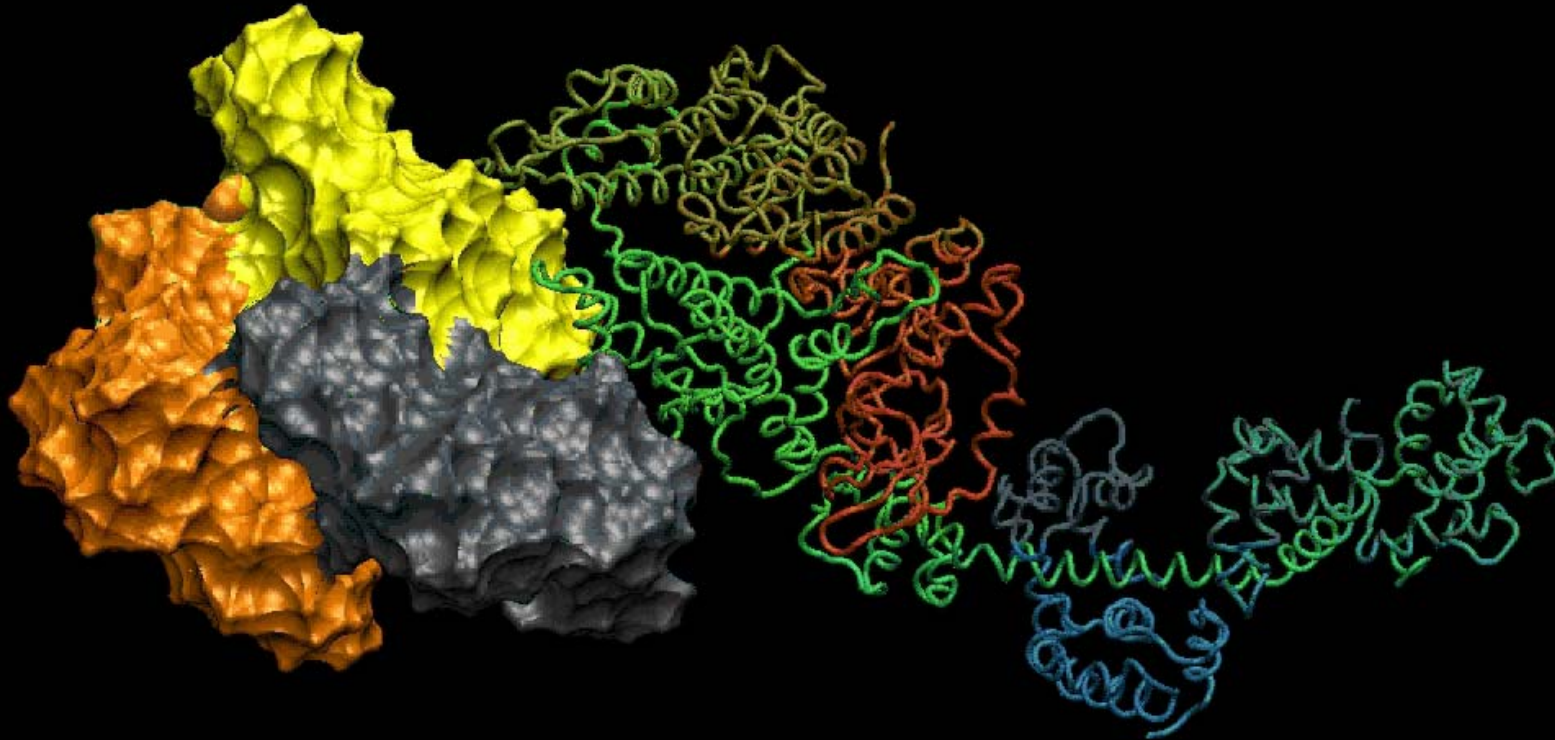
# Flexing of Myosin II



# Flexing of Myosin II



# Improved Actin Binding Surface



Cleft closure induced by actin binding

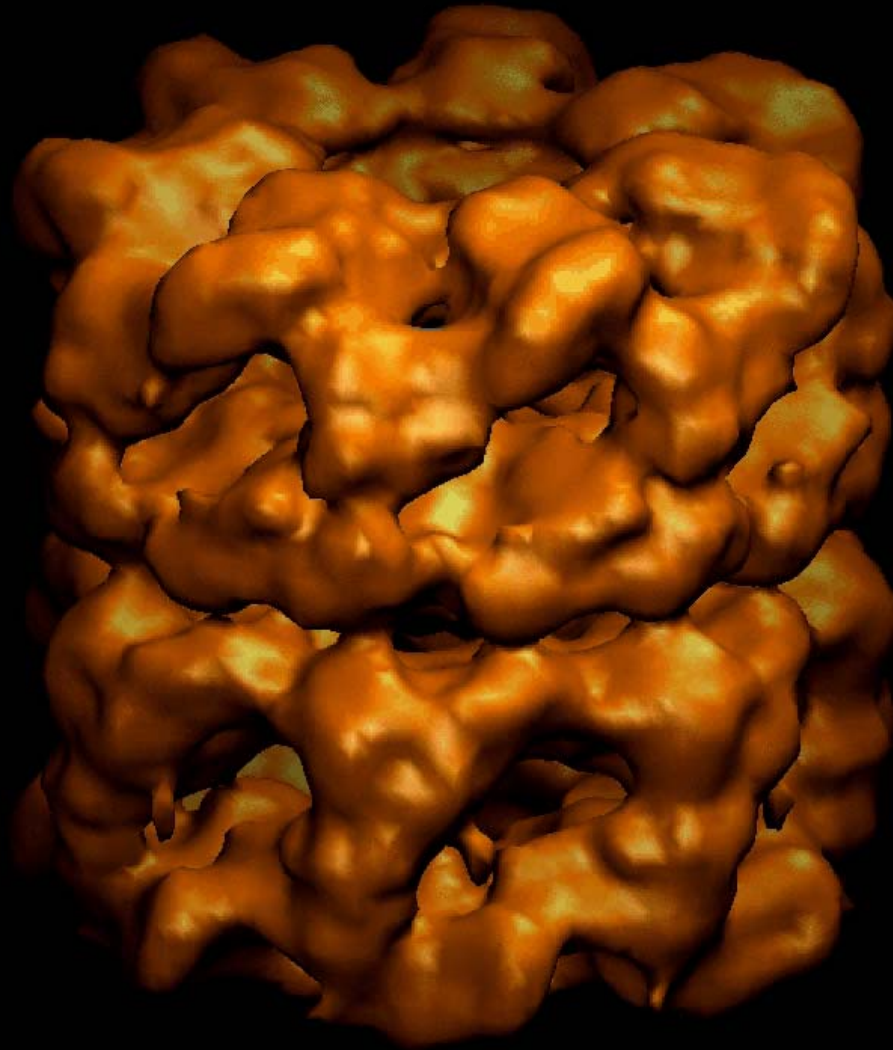
# Myosin Flexing Validation Results:

- Agreement ( $\sim 2\text{\AA}$  rmsd) between flexed myosin II and myosin V too close to be coincidental.
- MD flexible fitting reproduces entire allosteric mechanism (cleft closure, beta sheet twist, etc).
- Mechanism only partially observed with rigid-body fitting.
- Since myosin V was not used for modeling, this validates technique.



# GroEL Chaperonin

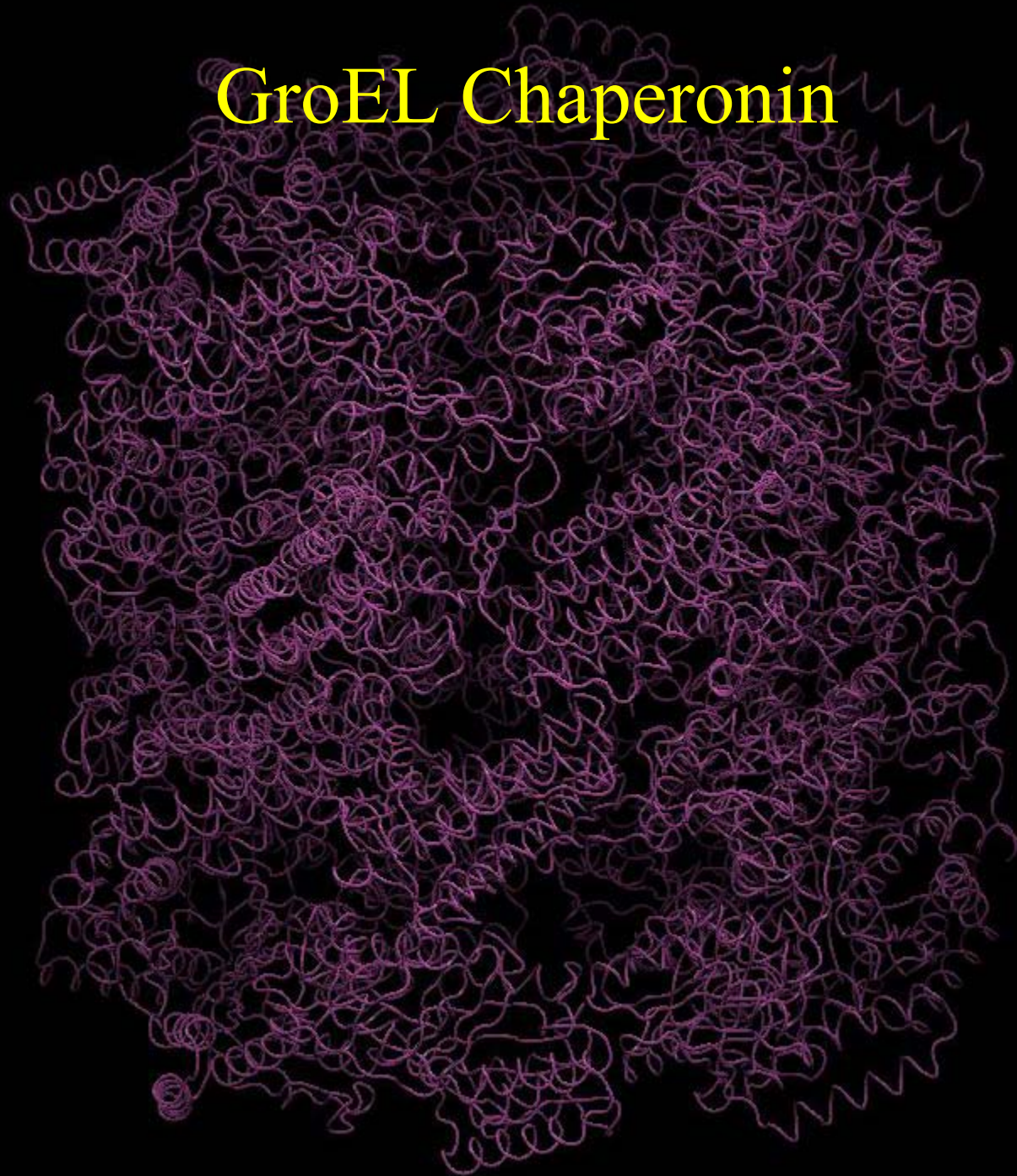
Dalia Segal,  
Sharon Wolf,  
Amnon Horovitz,  
Weizmann  
Institute, Israel



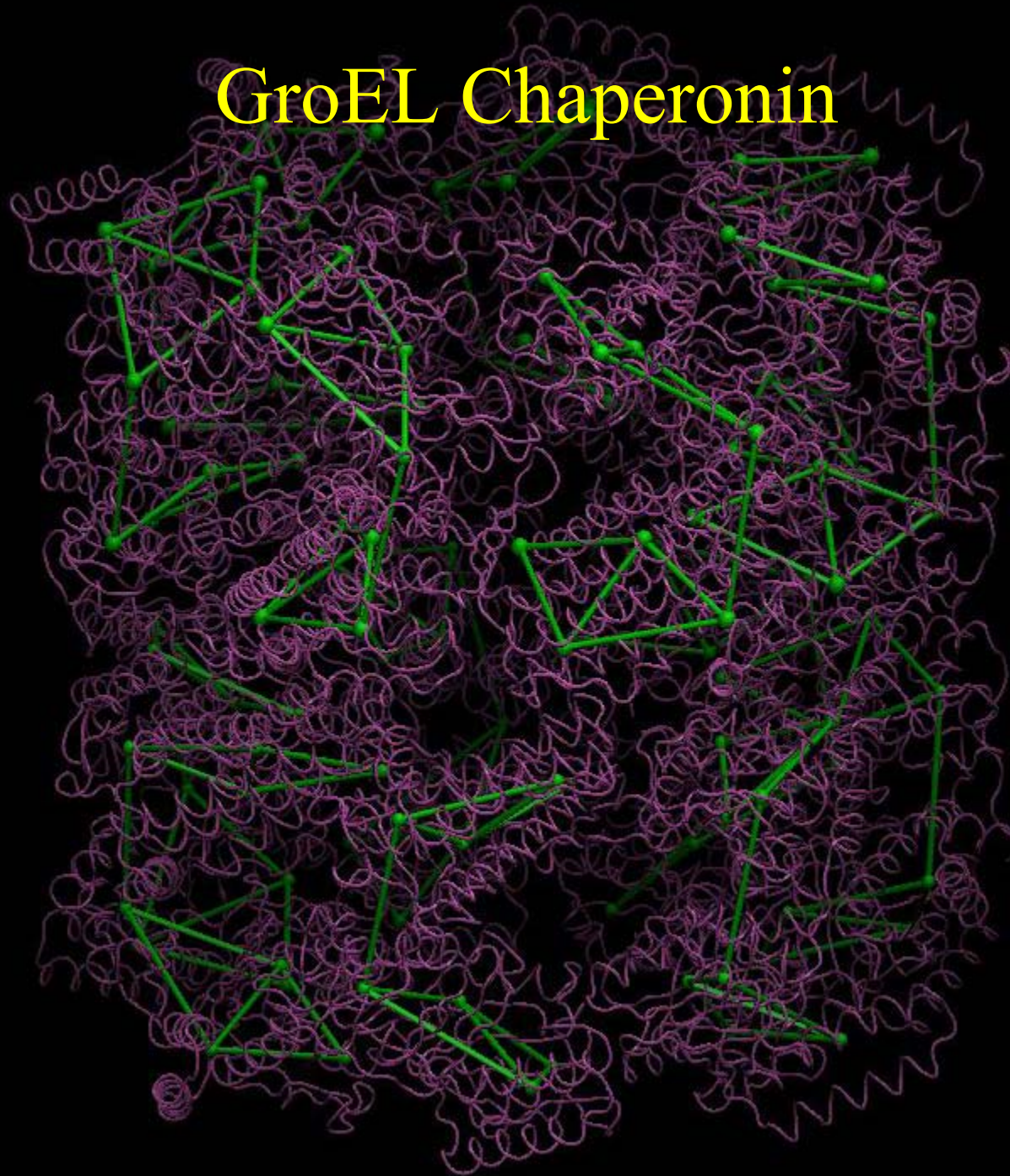
resolution  $\sim 14\text{\AA}$   
wild type  
(Sabil et al.)

& mutant

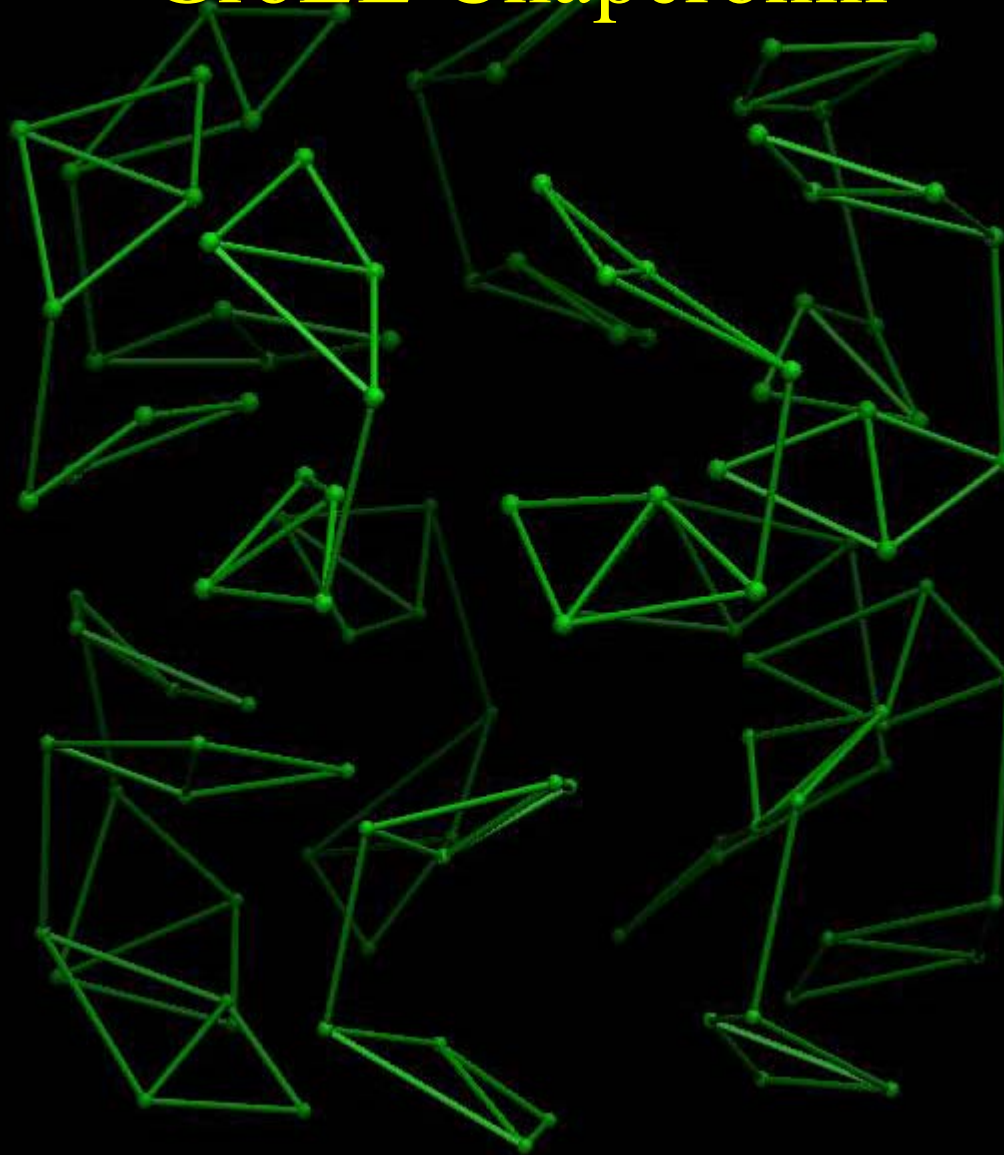
# GroEL Chaperonin



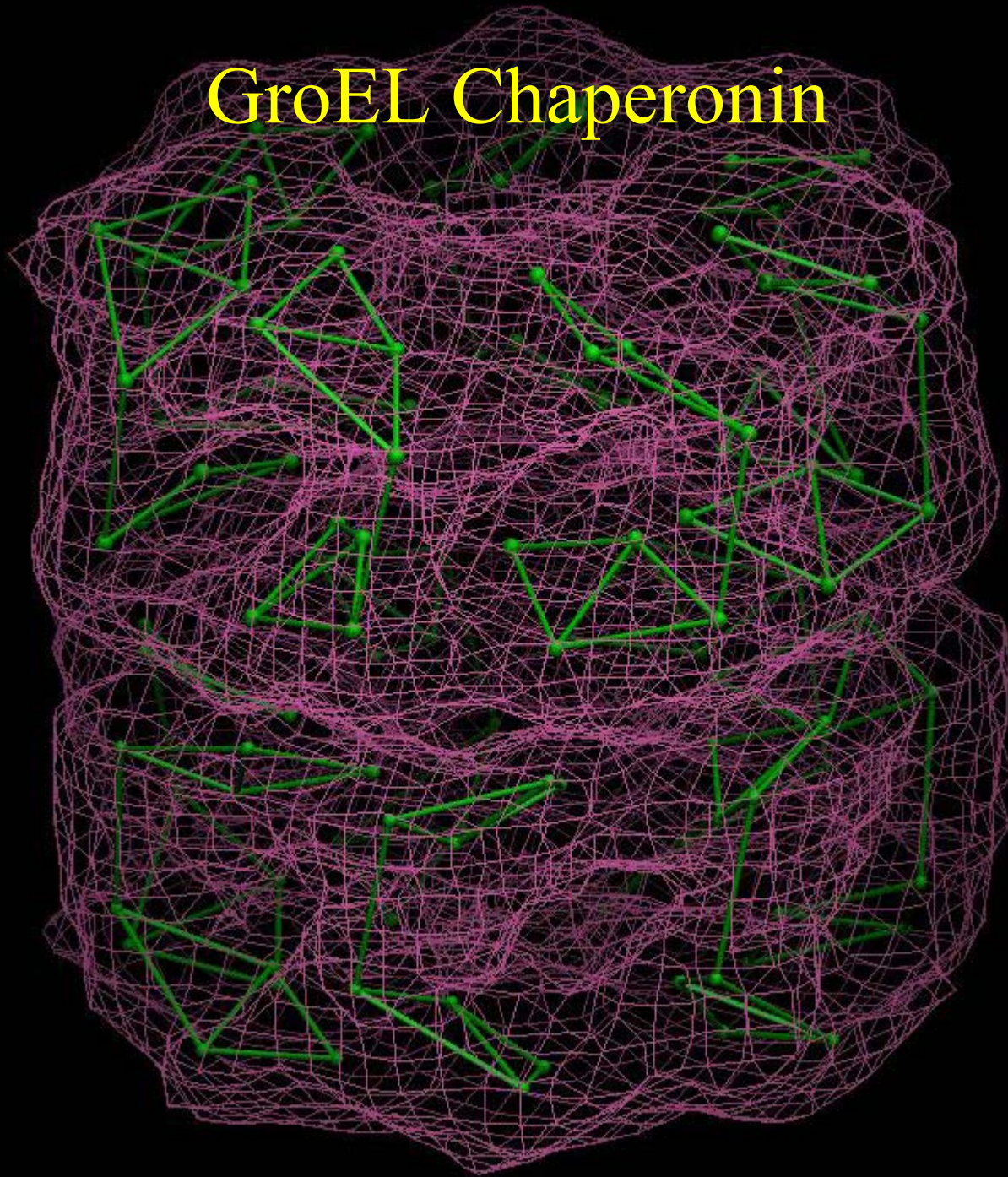
# GroEL Chaperonin



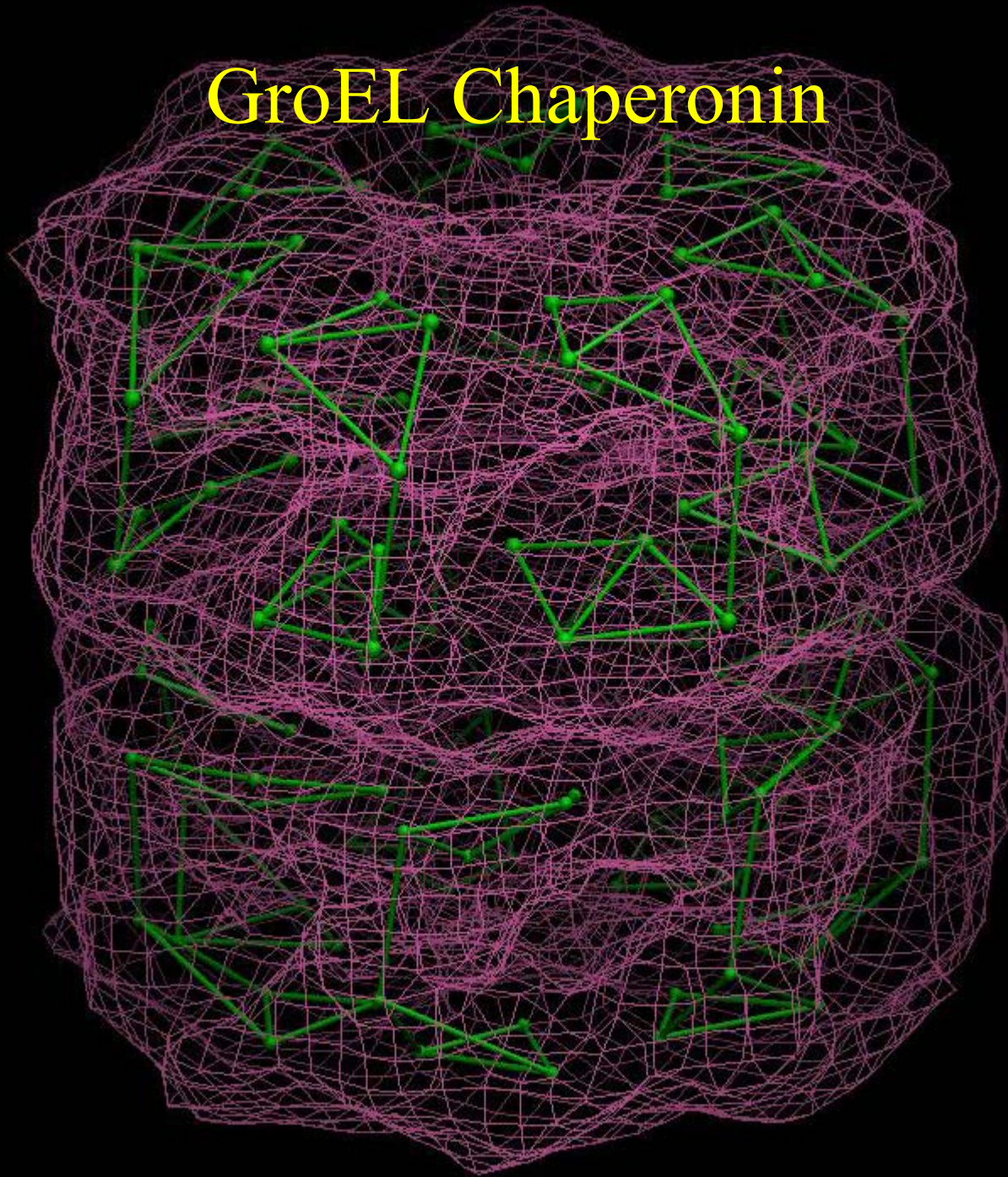
# GroEL Chaperonin



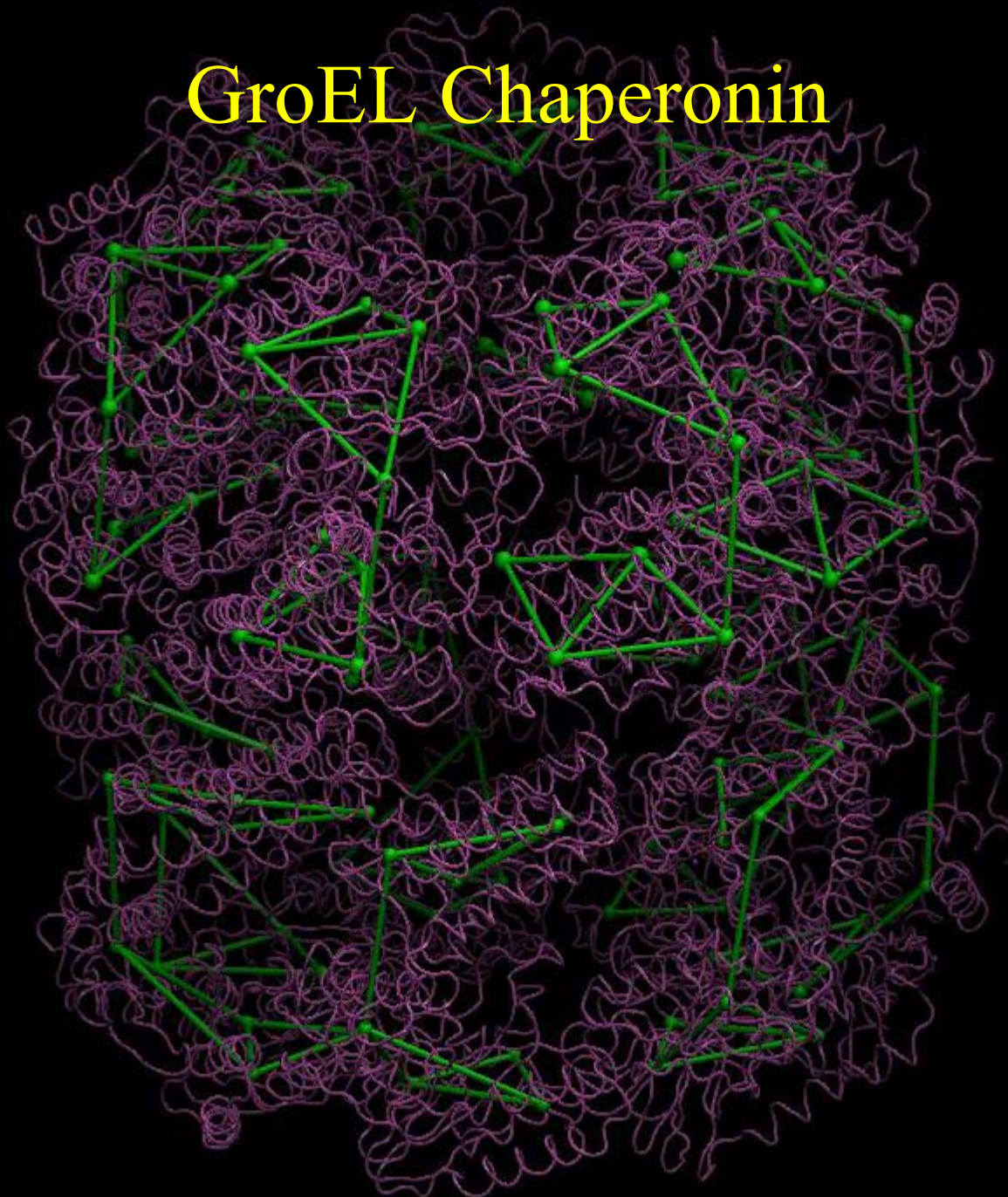
# GroEL Chaperonin



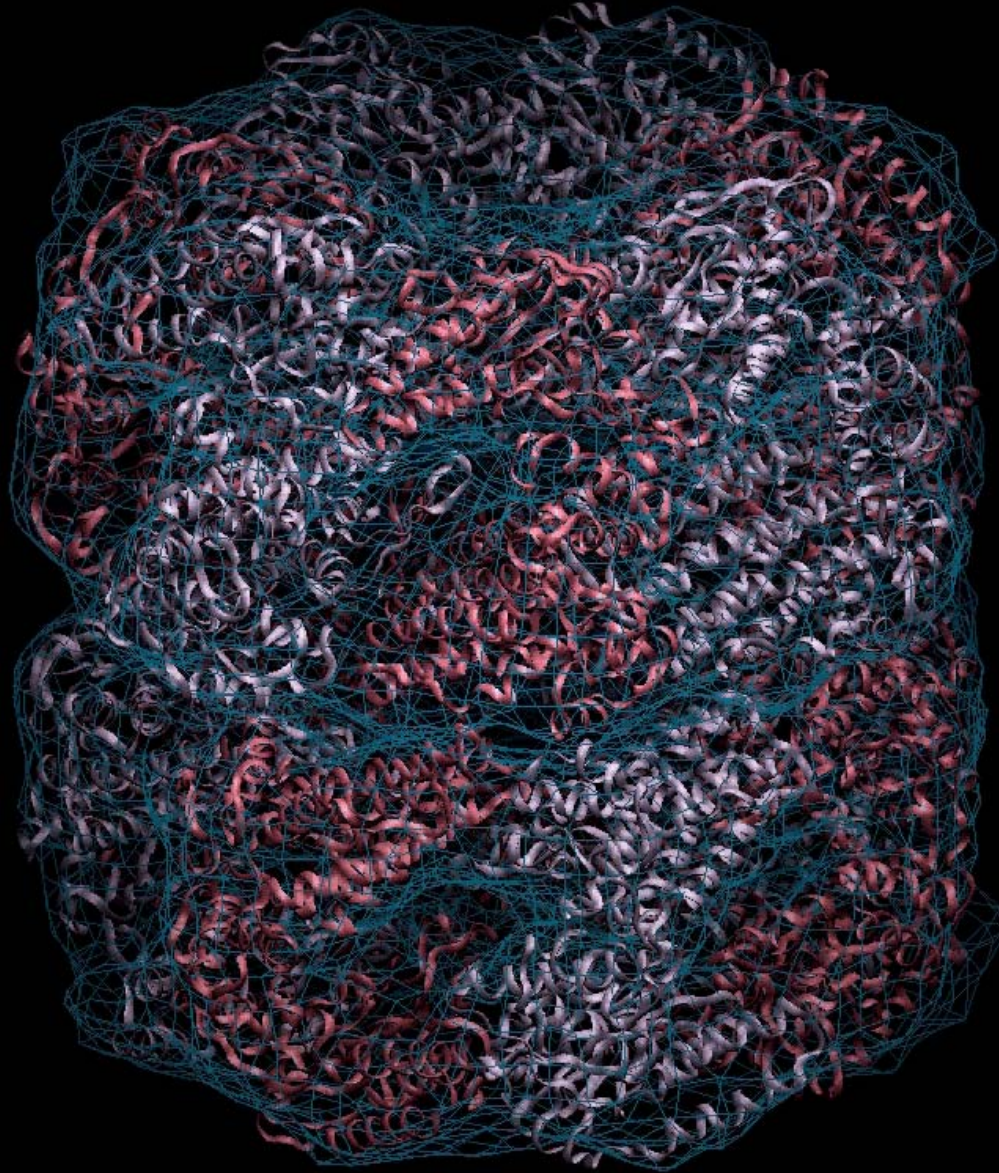
# GroEL Chaperonin



# GroEL Chaperonin



# GroEL Chaperonin





# Critical Assessment of MD Flexing

EM / Xtal Data	Resolution	Source	Precision (rmsd)
Myosin 2 Myosin 5	14Å	Schröder 2003	<b>2.0Å</b>
GroEL EM / Xtal WT	13Å	Saibil 2001	<b>3.0Å</b>
GroEL EM / Xtal WT	11Å	Ludtke 2003	<b>2.5Å</b>
GroEL EM / Xtal WT	6Å	Ludtke 2004	<b>2.0Å</b>
simulated EM / Xtal WT	6-14Å	simulated	<b>&lt;1.0Å</b>

# Resources and Further Reading

## **WWW:**

<http://situs.biomachina.org>

[http://http://situs.biomachina.org/tutorial\\_flex.html](http://http://situs.biomachina.org/tutorial_flex.html)

## **Papers:**

Willy Wriggers and Pablo Chacón. Structure, 2001, Vol. 9, pp. 779-788.

Willy Wriggers et al. Neurocomputing, 2004, Vol. 56, pp. 365-379.

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Dalia Segal, Sharon Wolf, Amnon Horovitz (Weizmann Institute, Israel)